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HANDBOOK OF SUPERSONIC AERODYNAMICS

Volume 4

Preface

A general preface to the entire Handbook of Supersonic Aerodynamics appears in Volume 1; therefore, the present preface applies specifically to the present issue of this portion of Volume 4 only.

This volume, when completed, will contain the following sections: Section 9 - Mutual Interference Phenomena, Section 10 - Static Stability, Section 11 - Dynamic Stability, and Section 12 - Aeroelastic Phenomena. Section 12 only is being issued at this time; the remaining sections for Volume 4 will be issued when completed.

Since the publication of Volumes 1 and 2 the contents of future volumes in the Handbook Series has been changed in accordance with the outline set forth on page iii of this preface under the caption: "Contents of Future Volumes in the Handbook of Supersonic Aerodynamics Series."

The numbering system for Volume 4 is the same as that used in Volume $\mathbf{2}$.

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Section 1 - Symbols and Nomenclature

Section 2 - Fundamental Equations and Formulae Section 3 - General Atmospheric Data

Section 4 - The Mechanics and Thermodynamics of Steady One-Dimensional Gas Flow

VOLUME 2* (NAVORD REPORT 1488, Unclassified)

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^{*} Published herewith.

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r = -0.2															1201-5b
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SECTION 12 - AEROELASTIC PHENOMENA

The following symbols are used in the material appearing on pages 1200-1 to 1208.2-58 of Section 12:

Primary Symbols

a	velocity of sound (free stream), ft/sec
b	semi-chord length, ft
c	location of aileron hinge line measured from mid- chord point in fractions of the semi-chord (+ aft)
c _h	translational spring constant per unit span, (lbs/ft) / (ft span)
$c_{1}^{}$, $c_{2}^{}$, $c_{3}^{}$	coefficients of determinantal equation
$^{ m C}_{ m Lh}$	part of supersonic flutter aerodynamic force co- efficient due to vertical displacement of the wing quarter-chord axis only
$^{ ext{C}}_{ ext{L}lpha}$	part of supersonic flutter aerodynamic force co- efficient due to rotational motion only
C _{Mh}	part of supersonic flutter aerodynamic moment co- efficient due to vertical displacement of the wing quarter-chord axis only
$^{ extsf{C}}_{ extbf{M}lpha}$	part of supersonic flutter aerodynamic moment co- efficient due to rotational motion only
C' _{Lh}	C _{Lh} when using the reduced frequency of the aileron
$\mathtt{C}'_{\mathtt{L}lpha}$	$^{ extsf{C}}_{ extsf{L}lpha}$ when using the reduced frequency of the aileron
C'Mh	$\mathbf{C}_{\mathbf{M}\mathbf{h}}$ when using the reduced frequency of the aileron
c_{Mlpha}	${ t C}_{ t Mlpha}$ when using the reduced frequency of the aileron
C'' _L h	$^{ m C}_{ m Lh}$ when using the reduced frequency of the wing forward of the aileron
$c_{\mathbf{L}lpha}^{"}$	$^{ extsf{C}}_{ extsf{L}lpha}$ when using the reduced frequency of the wing forward of the aileron
C''h	C _{Mh} when using the reduced frequency of the wing forward of the aileron
$^{\mathrm{C}^{\prime\prime}_{\mathbf{M}oldsymbol{lpha}}}$	$\mathbf{C}_{\mathbf{M}\Omega}$ when using the reduced frequency of the wing forward of the aileron
$^{\mathrm{c}}{}_{lpha}$	torsional spring constant per unit span, (ft-lbs/rad)/(ft span)

$c_{oldsymbol{eta}}$	torsional spring constant per unit span for aileron (ft-lbs/rad)/(ft span)
d	distance of elastic axis aft of quarter-chord line, ft
E	Young's modulus of elasticity
E _e	elastic energy
E _k	kinetic energy
F	half the rate of energy dissipation
${f g}_{f h}$	structural translational damping factor
$^{\mathrm{g}}\alpha$	structural torsional damping factor
$\mathbf{g}_{oldsymbol{eta}}$	structural torsional damping factor for aileron
G	shear modulus of elasticity
h	displacement of wing quarter-chord axis from the neutral position (+ downward), ft; also a general-ized displacement
h '	displacement of wing elastic axis from the neutral position (+ downward), ft
h _o	amplitude of h; also generalized amplitude of displacement
h'o	amplitude of h'
i	complex operator, $\sqrt{-1}$
I	section moment of inertia, ft^4
Ι'n	moment of inertia of system about elastic axis per unit span, lb-ft-sec $^2/(\mathrm{ft\ span})$
$\mathbf{I}_{oldsymbol{eta}}$	moment of inertia of aileron about hinge line per unit span, lb-ft-sec $^2/({ m ft\ span})$
J	effective section polar moment of inertia, ft^4
k	reduced frequency, $\omega b/V$, non-dimensional $\left[= \Omega \left(M^2 - 1 \right) / 2M^2 \right]$
$^{\mathbf{k}}\alpha$	reduced natural frequency in torsion, ω_{α} b/a
Į.	semi-span, ft
L	aerodynamic force per unit span, assumed at quarter- chord (+ downward, negative lift)#

The symbol L for aerodynamic force, as used in this section of the Handbook, for either primary or secondary concepts, is in the opposite direction to that of lift as customarily used in aerodynamics and as defined in Section 1 of this Handbook.

Lg	generalized aerodynamic force
L _h	part of aerodynamic force per unit span (L), assumed at quarter-chord point, due to various time derivatives of vertical displacement (h) of the wing quarter-chord axis
La	part of aerodynamic force per unit span (L), assumed at quarter-chord point, due to rotational displacement of the wing
L _β	aerodynamic force due to aileron per unit span
m	mass of moving system per unit span
^m 1	mass of wing per unit span $(m_1 = m \text{ in most applications})$
$^{\mathbf{n}_{oldsymbol{eta}}}oldsymbol{eta}$	mass of aileron per unit span
M	Mach number (free stream), V/a ; also moment per unit span (+ nose up)
Mg	generalized aerodynamic moment per unit span about elastic axis
M _h	part of aerodynamic moment per unit span (M) about the quarter-chord axis, due to vertical displacement (h) of the wing
$^{ ext{M}}_{lpha}$	part of aerodynamic moment per unit span (M) about the quarter-chord axis, due to rotational displacement of the wing
$\mathbf{M}_{oldsymbol{eta}}$	aerodynamic moment about hinge line due to the aileron
M'	aerodynamic moment per unit span, about the elastic axis
N	mechanical parameter, $I_{\alpha}^{\prime}/\pi\rho b^4$, non-dimensional
r	location of wing elastic axis measured from wing mid-chord point as a fraction of the semi-chord (+ aft), non-dimensional
S	mass unbalance per unit span, \max_{α} b
t	time, seconds
V	air velocity (free stream), ft/sec
×α	distance of center of gravity chordwise from elastic axis as a fraction of the semi-chord (+ aft), non-dimensional
×β	distance of center of gravity of aileron, measured from aileron hinge line, in fraction of the semichord (+ aft)
у	distance along span from wing root
α	displacement of wing in rotation from the neutral position, radians/(ft span), (+ nose up)

$a_{_{\mathrm{O}}}$	displacement of wing in rotation from the neutral position, normalized in three-dimensional case, per unit span, radians
β	<pre>angle of aileron with respect to chord line of wing (+ trailing edge downward)</pre>
$\Delta_0, \Delta_1, \Delta_2, \Delta_3$	coefficients in the third order stability equation (see Subsection 1207)
ρ	air density
μ	Mach angle = arc sin $1/M$ [: $cos^2 \mu = (M^2 - 1)/M^2$]
ϕ_1 , ϕ_2 , ϕ_3	functions of y defining the shapes of vibration modes
ω	circular frequency of oscillation, radians/sec
$\omega_{\mathbf{h}}$	uncoupled natural frequency in translation, $\sqrt{C_h/m}$, radians/sec
ω_{α}	uncoupled natural frequency in torsion, $\sqrt{C_{\alpha}/\Gamma_{\alpha}}$, radians/sec
$\omega_{oldsymbol{eta}}$	uncoupled natural frequency in torsion of aileron, $\sqrt{\frac{C_{\beta}}{I_{\beta}}}$, rad ans/sec
۵	frequency parameter, = $2k/\cos^2 \mu = \left[\frac{2M^2}{(M^2 - 1)}\right] k$

Auxiliary Symbols

The bar over a symbol $(\bar{\ })$ denotes the real component of the complex quantity designated by the associated symbol.

The asterisk (*), used as a superscript, denotes the imaginary component of the complex quantity designated by the associated symbol.

The dot (') is used to denote differentiation with respect to time, thus $\dot{\alpha}=\mathrm{d}\alpha/\mathrm{d}t$ and $\ddot{\alpha}=\mathrm{d}^2\alpha/\mathrm{d}t^2$.

SECTION 12 - AEROELASTIC PHENOMENA

This section of the Handbook of Supersonic Aerodynamics was prepared at the Applied Physics Laboratory of The Johns Hopkins University, with the cooperation of the Bumblebee Committee on Aeroelasticity and Structural Dynamics. Members of this committee were as follows:

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The original draft of this section was prepared for the Committee by T. K. Riggs in accordance with the Committee's recommendations and suggestions. The final draft was prepared by C. N. Warfield who gratefully acknowledges the helpful comments and suggestions by the members of the Committee and by his colleagues, F. K. Hill, J. P. Kearns, R. M. Mains, and E. Shotland—and the helpful assistance of Mrs. Corine Carwile Bloss who checked many of the equations and the numerical results, computed the numerical example, and prepared the copy for the final graphs.

The tables of flutter coefficients which appear in this section were especially computed, under the supervision of E. C. Kennedy, at the Ordnance Aerophysics Laboratory on International Business Machines Corporation equipment for initial publication in this Handbook.

1200 Introduction

1200.1 General Scope of Section

In this section of the Handbook there are presented certain tables and graphs that may be used, on the basis of flutter considerations, in the design of guided missiles. In addition there is included here a brief treatment of certain theoretical aspects of flutter in the supersonic regime. This treatment includes a derivation of one of the equations for flutter of airfoils in supersonic flow, namely that for torsional flutter of a two-dimensional (infinite) wing.

The tables above referred to (Tables 1208.2) contain the real and imaginary parts of the supersonic force and moment flutter coefficients for airfoils. These flutter coefficients are equivalent to those originally defined by Borbely (Reference 12-1).

Presently employed by Engineering Research Associates, Inc.

These tables were computed by use of a recursion formula that was devised by E. C. Kennedy, and they are tabulated as a function of a frequency parameter (Ω) for each of several values of Mach number (M). The parameter (Ω) is related to the reduced frequency (k) and to the Mach num-

ber (M) by the equation $\Omega = \left[2M^2/(M^2 - 1)\right]k$, and a table based on this relationship is presented (Table 1208.1). The reduced frequency is the ratio between the circular frequency of oscillation (ω), in radians per second, and the number of times per second that the wing, due to its forward speed (V), traverses a distance equal to its semi-chord (b).

The tabular values for the flutter coefficients in the great majority of cases are believed to be accurate to within one in the last digit, and in no case is the tabulated value in error by more than two in the last digit. The Mach number range covered is from 1.1 to 12 while the value of Ω ranges from 0.01 to 20. The increments in both M and Ω are in general smaller than in existing similar tables. Because supersonic flutter computations sometimes involve relatively small differences of coefficients, these coefficients have been computed and tabulated in most cases to eight significant figures, although in many applications three or four digits will suffice.

Also included in this section are brief treatments of binary flutter (wing torsion and bending modes) and of ternary flutter (wing torsion, first-and second-bending modes, aileron and wing torsion and bending modes). Both two-dimensional (infinite span) and three-dimensional (finite span) airfoils are analyzed. Brief discussions are given of certain methods of solution for the higher order determinantal equations that appear in some of these analyses. A brief mention of the use of coupled and of uncoupled vibration modes in supersonic flutter is included.

For the purpose of familiarizing the non-specialist with the technique of flutter computations, this section includes a numerical example of an application of the supersonic flutter coefficients. This example is for two-dimensional binary flutter, and is based on the method presented in the Air Materiel Center report entitled "Application of Three-Dimensional Flutter Theory to Aircraft Structures" (Reference 12-2).

In addition to the list of cited references, there is included at the end of this subsection a bibliography of the more pertinent literature on supersonic flutter.

The effects of body motion and the flexibility of attachment of the wing are not discussed in this section since these effects are adequately covered in the literature on subsonic flutter (Reference 12-2). Finite span effects, resulting in a loss of litt force at the wing tip, are not taken into account; however, theoretical studies are available on this subject (References 12-3, 12-4, 12-5, 12-6 and 12-7). Empirical corrections may be used to account for tip effects with some degree of reliability.

The effect of sweepback on the fluctuating aerodynamic forces is somewhat more complicated than the effect on the static lift and moment coefficients for the same type of wing. These sweepback effects are discussed in Reference 12-3. It is possible to calculate the effects of sweepback on the elastic properties of a wing by the use of approximations, provided the aspect ratio is sufficiently high. Whenever a completed structure is available its elastic properties may be obtained from ground vibration tests.

1200.2 Basic Concepts

An airframe at rest on the ground in still air will respond to an impulse in one of three ways. Depending upon the amount of structural damping present it will either execute a series of periodic oscillations of diminishing amplitude, or return to its initial state of rest in the shortest possible time (critically damped), or return more slowly to a state of rest.

If the airframe at rest is subjected to a sinusoidal forcing function it will, after passing through a transient condition, settle into a steady-state vibratory motion with a frequency the same as that of the forcing function, and whose deflections and amplitude of vibration are determined by the applied frequency, as well as by the elastic, inertial, and damping characteristics of the airframe structure.

Since fluctuating aerodynamic forces result from oscillatory motions of an airframe, the response of an airframe to an impulse or sinusoidal forcing function will be determined by these fluctuating aerodynamic forces as well as by the characteristics of the airframe structure. If the phase relationship of the aerodynamic forces is such as to reinforce the motions producing them, then a condition of self-sustaining oscillation is possible. This condition gives rise to what is known as flutter. The flutter frequency is determined by the flight Mach number as well as by the structural characteristics of the airframe.

In flutter analyses computations are made for the critical flutter condition in which the amplitude of vibration tends to remain constant. When the amplitude of vibration increases the condition is considered unsafe; when the amplitude decreases it is considered safe.

The boundary between the safe and unsafe flutter conditions may be identified by investigating the equations of motion. An approximate measure of the margin of safety may be given by the value of the critical structural damping factor computed for the airfoil structure with the aid of the herein tabulated aerodynamic flutter coefficients. Then this value can be compared with the actual structural damping factor obtained experimentally by a vibration test, or by estimation based on experience. Or, the degree of safety from flutter may be estimated by considering the distance between the point on a suitable chart describing the known properties of the wing and the line on the same chart, based on the herein tabulated flutter coefficients, which designates the boundary between the "safe" and "unsafe" regions.

In flutter analyses the computations are based on the frequency, shape and phase relationship of certain vibration modes that are characteristic of the structure. Ideally, the principal* modes as they occur in flight under the aerodynamic conditions that exist during critical flutter oscillations would be used in these flutter analyses. Theoretically, in the case of three-dimensional bodies, there are an infinite number of possible vibration modes. For practical purposes, however, the deformation of an airframe during a state of critical flutter may be assumed to be a combination of the deflections due to the first two, three, or possibly four of the principal modes of vibration—these principal modes correspond to the lower frequencies at which the structure vibrates in resonance. Approximations to these desired modes may be obtained by analytical methods, or by measurements made on the airframe while vibrating either at rest on the ground in still air, or while in flight, or by other experimental means. Reference 12-8 demonstrates the feasibility of basing the analyses upon the actual coupled modes of vibration rather than upon the fictional uncoupled modes.

Sometimes referred to in the literature on flutter as the characteristic, natural, or normal (coupled) modes.

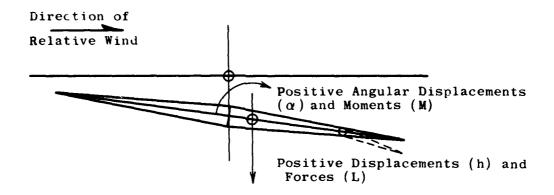
Introduction

It has been found that flutter may occur in the torsional mode without the presence of a flexure component. This is because at certain frequencies and elastic axis positions the aerodynamic damping is negative, that is, the imaginary component of the aerodynamic moment acts in phase with the angular velocity so as to accelerate the wing in rotation rather than retard it. However, it has been shown that such pure torsional flutter cannot occur at Mach numbers greater than 1.58 (Reference 12-9) for slow oscillations, and the limiting Mach numbers for more rapid oscillations do not differ much from this slow oscillation value.

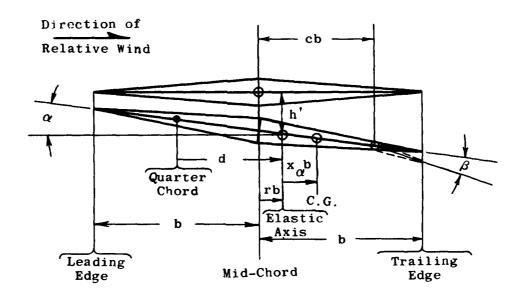
If an unswept wing were to oscillate in bending only, with no rotary motion, then the aerodynamic damping would always be positive, and no flutter involving this mode alone will occur.

1201 Two-Dimensional Torsional Flutter

When an airfoil oscillates in a torsional mode only, various moments about the axis of rotation are involved. For a unit span of the airfoil the elastic restoring moment will be $-C_{\alpha}\alpha$ (cf. symbols list on pages 1200-1 and 1200-3, and Figure 1201-1), and the structural damping moment is represented as a fraction, g_{α} , of the elastic restoring moment, rotated in



a. Directions (The notation as to directions is the same as that of the NACA and the American Standards Association's "Letter Symbols for Aeronautical Sciences, Z-10.7, 1950")



b. Symbols

Figure 1201-1 TWO-DIMENSIONAL WING NOTATIONS

phase so as to lead the latter by 90 degrees. The resultant of these two moments may be represented by $-(1+ig_{\alpha})C_{\alpha}\alpha$, where i is the complex operator $\sqrt{-1}$. The inertial moment per unit span is expressed by $-I_{\alpha}^{'}\ddot{\alpha}$ ' and the aerodynamic moment per unit span about the elastic axis is represented here as M'. The sum of these moments is zero, and consequently the aerodynamic moment may be expressed by

$$\mathbf{M'} = \mathbf{I'}_{\alpha}\ddot{\alpha} + (1 + \mathbf{ig}_{\alpha}) \mathbf{C}_{\alpha}\alpha \qquad (1201-1)$$

Consider now the contribution to the aerodynamic moment M' about the elastic axis per unit span due to the rotational displacement α of the wing from the neutral position. If we let the positive aerodynamic force (that is, negative lift L), due to this angular displacement, act at a distance d forward of the elastic axis, and let M represent the aerodynamic pitching moment about the line passing through the point of application of the aerodynamic force L , it is obvious that such a rotational displacement contributes to the moment about the elastic axis an amount (see Figure 1201-2)

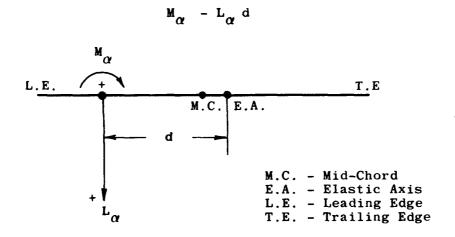


Figure 1201-2 FORCE AND MOMENT NOTATIONS

Likewise, in view of the effect of various time derivatives of displacement (h) of the wing quarter-chord axis which contribute \mathbf{M}_h and \mathbf{L}_h relative to the quarter-chord, it similarly follows that such a translatory displacement contributes to the moment about the elastic axis an amount

$$M_h - L_h d$$

The total aerodynamic moment about the elastic axis, due to both rotational and translatory motions, is therefore

$$M' = (M_{\alpha} - L_{\alpha} d) + (M_{h} - L_{h} d)$$
 (1201-2)

Using aerodynamic force and moment flutter coefficients that are defined by $\begin{tabular}{ll} \hline \end{tabular} \label{table_equation}$

$$C_{Lh} = \frac{L_h}{\pi \rho b^2 \omega^2 h}$$

$$C_{L\alpha} = \frac{L_{\alpha}}{\pi \rho b^3 \omega^2 \alpha}$$

$$C_{Mh} = \frac{M_h}{\pi \rho b^3 \omega^2 h}$$

$$C_{M\alpha} = \frac{M_{\alpha}}{\pi \rho b^4 \omega^2 \alpha}$$
(1201-3)

one finds that Equation 1201-2 becomes

$$M' = \pi \rho b^4 \omega^2 \left[C_{M\alpha}^{\alpha} - C_{L\alpha}^{\alpha} \frac{d}{b} \alpha + C_{Mh}^{\alpha} \frac{h}{b} - C_{Lh}^{\alpha} \frac{hd}{b^2} \right]$$

$$(1201-4)$$

If, as is customary in subsonic flutter analyses, we assume the lift force to act at the quarter-chord point then

$$d = b \left(\frac{1}{2} + r\right)$$

and we find that Equation 1201-4 becomes

$$M' = \pi \rho b^{4} \omega^{2} \left[C_{M\alpha} \alpha - C_{L\alpha} \left(\frac{1}{2} + r \right) \alpha + C_{Mh} \left(\frac{1}{2} + r \right) \frac{h}{d} - C_{Lh} \left(\frac{1}{2} + r \right)^{2} \frac{h}{d} \right]$$
(1201-5)

(Note- This equation for two-dimensional flutter could have been obtained directly from the Borbely-Possio equation (1203-8) by using the relation $h' = h + \alpha d$; cf. Figure 1201-3.)

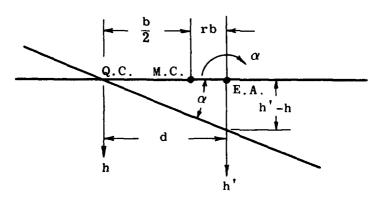


Figure 1201-3 DISPLACEMENT NOTATIONS

To transform the motion parameters from the quarter-chord axis to the elastic axis (see Figure 1201-3), let

$$h' = h + \alpha rd \qquad (1201-6)$$

For the torsional mode only h' = 0; and therefore Equation 1201-6 reduces to

$$\frac{h}{d} = -\alpha \tag{1201-7}$$

Equation 1201-5 then becomes

$$M' = \pi \rho b^4 \omega^2 \alpha \left[C_{M\alpha} - C_{L\alpha} \left(\frac{1}{2} + r \right) - C_{Mh} \left(\frac{1}{2} + r \right) + C_{Lh} \left(\frac{1}{2} + r \right)^2 \right]$$
(1201-8)

For harmonic oscillatory motion of rotation, we may write

$$\alpha = \alpha_0 e^{i\omega t} \tag{1201-9}$$

Differentiating α (Equation 1201-9) twice with respect to time, and substituting α and its second time derivative, and Equation 1201-8 into Equation 1201-1, and substituting $\omega_{\alpha}^{\ 2}$ for $C_{\alpha}/I_{\alpha}^{'}$, one obtains

$$\left(\frac{\omega_{\alpha}}{\omega}\right)^{2} (1 + ig_{\alpha}) - 1 + \frac{\pi \rho b^{4}}{I_{\alpha}^{*}} \left[- c_{M\alpha} - c_{Lh} \left(\frac{1}{2} + r\right)^{2} + c_{L\alpha} \left(\frac{1}{2} + r\right) + c_{Lm} \left(\frac{1}{2} + r\right) \right] = 0$$
 (1201-10)

(Note- This equation for two-dimensional torsional flutter could have been obtained from the more general determinantal equation for two-dimensional binary flexure-torsion flutter (Equation 1202-9), by equating the $M_{22} + A_{22}$ element to zero, in which M_{22} and A_{22} are defined by Equations 1202-7 and 1202-10, respectively.)

For convenience, the real and imaginary parts of the aerodynamic coefficient term (i.e., the term included in the brackets) are represented hereafter by \bar{A}_{22} and A_{22}^* respectively, whence

$$\overline{A}_{22} = -\overline{C}_{M\alpha} - \overline{C}_{Lh} \left(\frac{1}{2} + r\right)^2 + \overline{C}_{L\alpha} \left(\frac{1}{2} + r\right) + \overline{C}_{Mh} \left(\frac{1}{2} + r\right)$$
and
$$A_{22}^* = -C_{M\alpha}^* - C_{Lh}^* \left(\frac{1}{2} + r\right)^2 + C_{L\alpha}^* \left(\frac{1}{2} + r\right) + C_{Mh}^* \left(\frac{1}{2} + r\right)$$
(1201-11)

The reason for the use of the subscript 22 will be apparent in the subsection on binary flutter, 1202. With this symbolism, Equation 1201-10 becomes

$$\left(\frac{\omega_{\alpha}}{\omega}\right)^{2}\left(1+ig_{\alpha}\right)-1+\frac{\pi\rho b^{4}}{i_{\alpha}^{*}}\left(\overline{A}_{22}+iA_{22}^{*}\right)=0 \qquad (1201-12)$$

Equation 1201-12 may be written as two equations: one including only the real terms, and the other only the imaginary terms. When this is done and the substitution N = $I_{\alpha}^{*}/\pi\rho b^{4}$ is made, the following equations may be obtained:

$$\left(\frac{\omega_{\alpha}}{\omega}\right)^{2} = 1 - \frac{\overline{A}}{N}$$
 (1201-13)

$$g_{\alpha} = \frac{-A^*_{22}}{N - A_{22}}$$
 (1201-14)

These equations for two-dimensional torsional flutter may be used for a quick survey of the flutter characteristics of a finite wing if one first obtains an approximate spanwise average value for each of the parameters involved, e.g. I'_{\alpha}, b, r and ω_{α} . However, the use of such spanwise average values in the equations for two-dimensional torsional flutter obviously cannot be relied upon for precise results.

When values of ω and M, and therefore also of \overline{A}_{22} and A_{22}^* for a certain elastic axis location (r), are found which satisfy Equations 1201-13 and 1201-14, the conditions for borderline two-dimensional torsional flutter are defined for the conditions represented by the parameters $I'_{\alpha}/\pi\rho b^4$ and $\omega_{\alpha}b/a$. The latter term, $\omega_{\alpha}b/a$, is hereafter referred to as the "reduced natural frequency," k_{\alpha}.

Several methods may be used to obtain significant data from these equations, two of which are described below.

Method 1. Computation of torsional damping factor g_{α} .

(a) At each Mach number of interest, using the mechanical parameter N and the elastic axis location r of the wing, determine by means of Equation 1201-13, for a series of values of the frequency parameter Ω , the corresponding values of ω_{α} . Then the reduced natural frequency \mathbf{k}_{α} can be determined by

$$k_{\alpha} = Mk \left(\frac{\omega_{\alpha}}{\omega}\right) \qquad (1201-15)$$

where k, the reduced frequency, is given by

$$k = \Omega \left(\frac{M^2 - 1}{2M^2} \right)$$

- (b) Likewise, by means of Equation 1201-14, one can determine the values of ${\bf g}_{\alpha}$ corresponding to the same values of ${\bf \Omega}$ that were used in (a), for the same combination of values of ${\bf M}$, r, and N.
- (c) For each value of that was used in parts (a) and (b) there has been obtained a pair of values of \mathbf{g}_{α} and of \mathbf{k}_{α} . These pairs of values can then be plotted as in Figures 1201-4a, b, c and d, which represent four combinations of fairly extreme values of r and of N. Of course, figures of this type can be prepared for any desired combination of values for r and N.

If the borderline damping factor \mathbf{g}_{α} thus determined is negative or less positive than the actual structural torsional damping factor for the structure, as determined by damped vibration test data, safety from flutter is indicated; if it is positive and greater than the experimental value, unsafe flutter is indicated.

Method 2. Computation, assuming the torsional damping factor \mathbf{g}_{α} is zero.

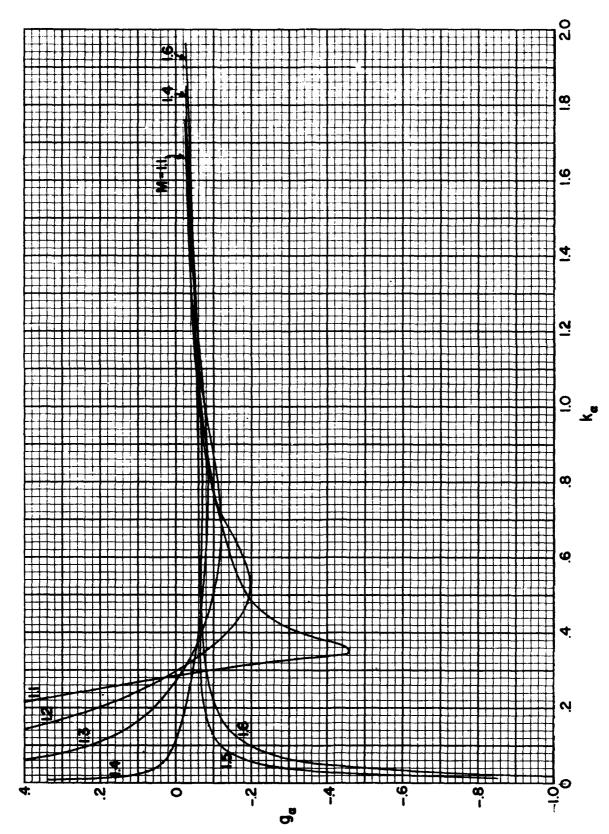
If one is interested in determining only a conservative indication of the flutter characteristic of the structure (that is, whether or not the structural parameters are such as to indicate no flutter even if the structural torsional damping factor \mathbf{g}_{α} is zero), then it is necessary to determine from Equations 1201-13 and 1201-14 what combinations of the several parameters correspond to the conservative condition represented by $\mathbf{g}_{\alpha}=0$. This has been computed for various practical ranges of the several parameters and the results are given in Figures 1201-5. The dashed portions of these curves represent extrapolated values only. In these figures regions above the curves are free from flutter, but below these curves the likelihood of flutter occurring increases with increasing distances. For example, with a structure for which $\mathbf{r}=0$, N=20 and $\mathbf{k}_{\alpha}=0.25$, it is evident that flutter is probable only at Mach numbers between 1.133 and 1.311.

Other methods of obtaining and presenting results for single-degree-of-freedom (torsional) flutter are described in References 12-10 and 12-11.

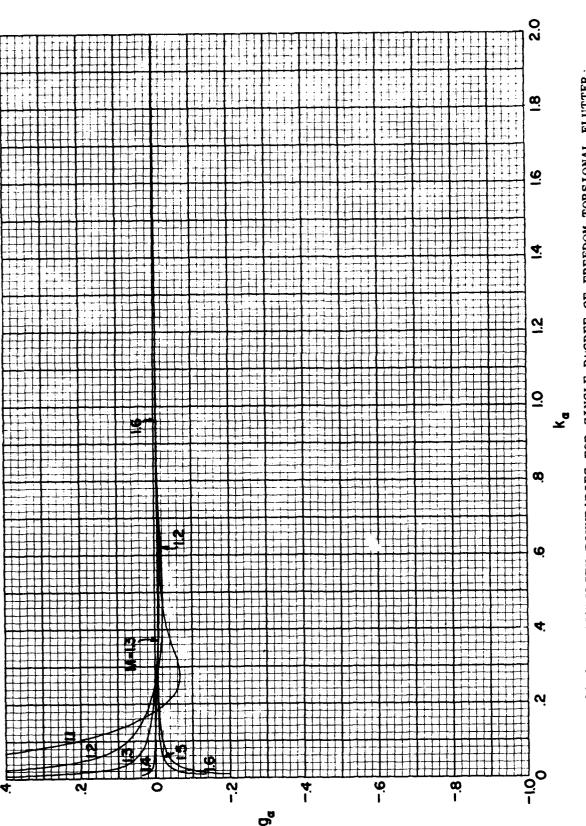
The following facts are important in making a decision as to whether or not an analysis for single-degree-of-freedom (torsional) flutter is adequate in any specific situation:

- (1) For elastic axis positions close to the mid-chord, static divergence (when second-order shift in aerodynamic center location is taken into account) may be more critical than torsional fultter.
- (2) At low supersonic Mach numbers the flow may be transonic in character, and the applicability of linearized supersonic aerodynamic forces used in these analyses would then be in doubt.
- (3) For $(\omega_h/\omega_{\alpha})$ < 1, the binary flutter stability boundary will usually be more critical than these torsional ones.

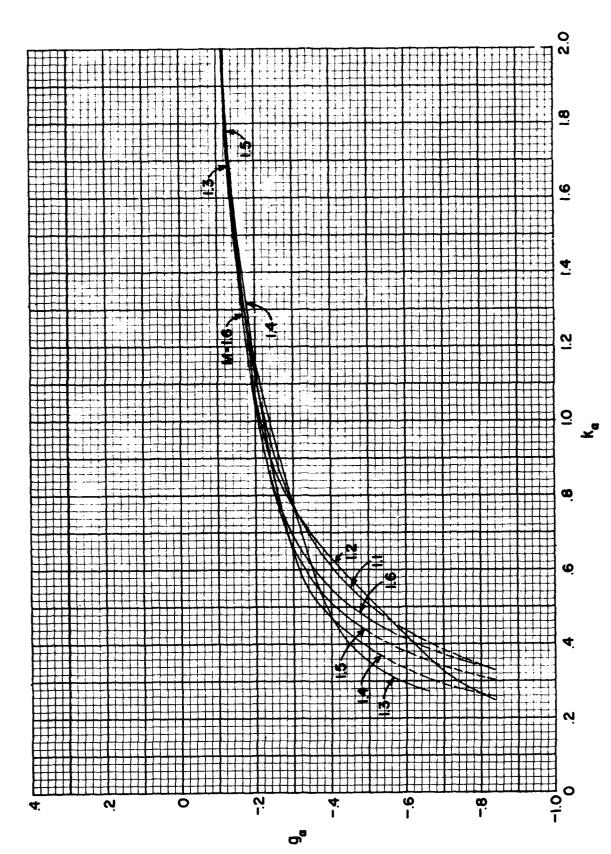
For binary flexure-torsion flutter an approximation can be obtained by the method described in Subsection 1202; and for actual finite wings more reliable results can be obtained by means of the equations for three-dimensional binary flexure-torsion flutter that are presented in Subsection 1203.



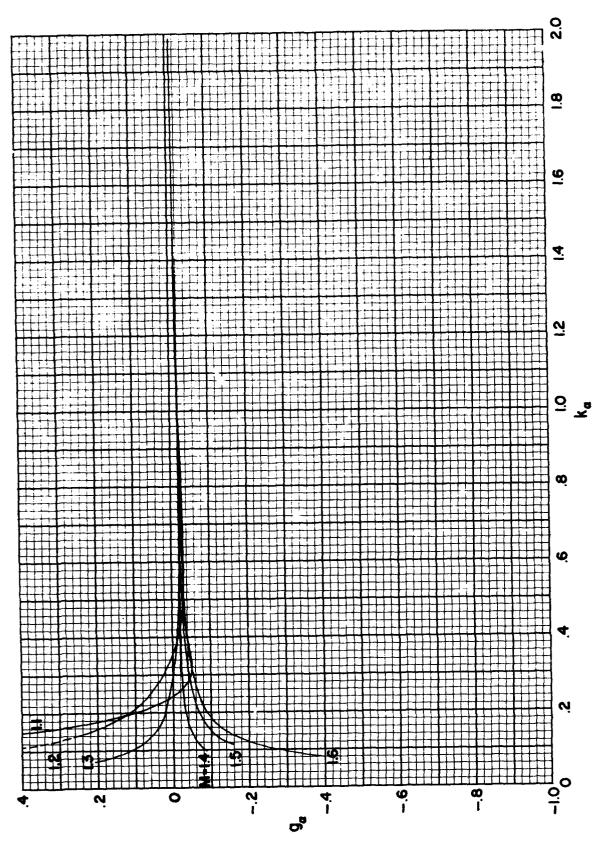
STABILITY BOUNDARIES FOR SINGLE-DEGREE-OF-FREEDOM TORSIONAL FLUTTER; ${\bf g}_{\alpha}$ vs ${\bf k}_{\alpha}$, MACH NUMBER (M) INDEPENDENT. ${\bf r}$ = 0 and N = 10 Figure 1201-4a



STABILITY BOUNDARIES FOR SINGLE-DEGREE-OF-FREEDOM TORSIONAL FLUTTER \mathbf{g}_{α} vs \mathbf{k}_{α} , MACH NUMBER (M) INDEPENDENT. \mathbf{r} = 0 and N = 100



STABILITY BOUNDARIES FOR SINGLE-DEGREE-OF-FREEDOM TORSIONAL FLUTTER g vs k_{∞} , MACH NUMBER (M) INDEPENDENT. r=-1.2 and N=10Figure 1201-4c



SINGLE-DEGREE-OF-FREEDOM TORSIONAL FLUTTER (M) INDEPENDENT. r = -1.2 and N = 100 MACH NUMBER (M) INDEPENDENT. STABILITY BOUNDARIES FOR g Figure 1201-4d

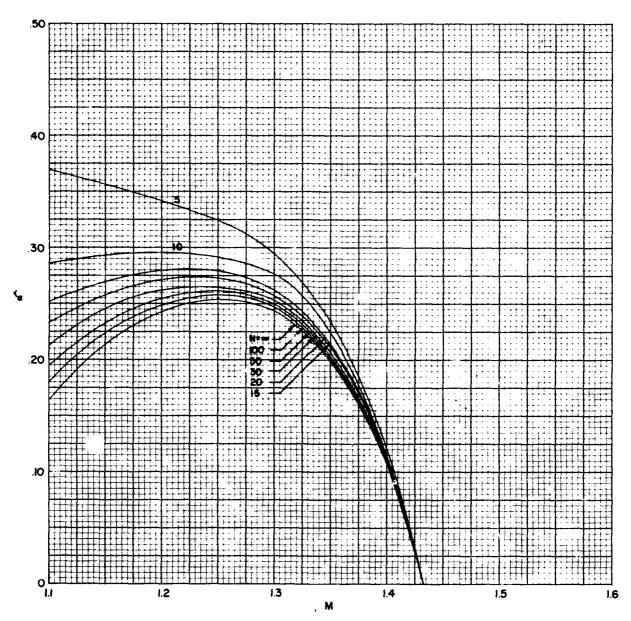


Figure 1201-5a STABILITY BOUNDARIES FOR SINGLE-DEGREE-OF-FREEDOM TORSIONAL FLUTTER FOR ZERO DAMPING ($g_{\alpha} = 0$).

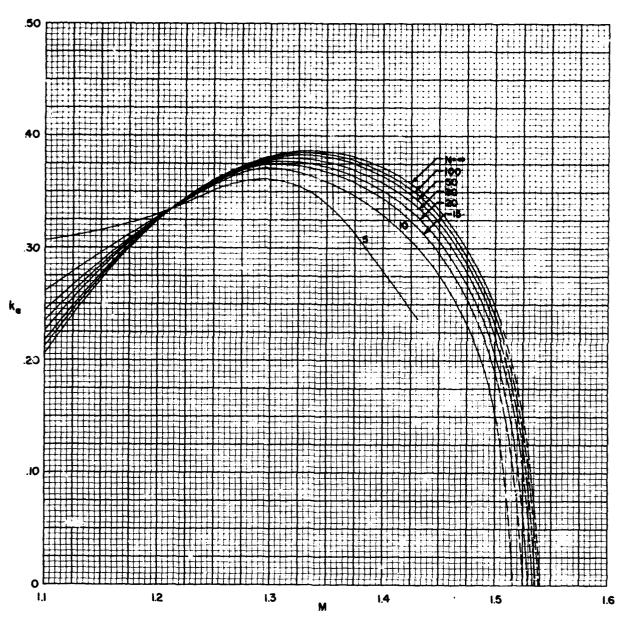


Figure 1201-5b STABILITY BOUNDARIES FOR SINGLE-DEGREE-OF-FREEDOM TORSIONAL FLUTTER FOR ZERO DAMPING ($g_{\alpha}=0$). r=-0.2

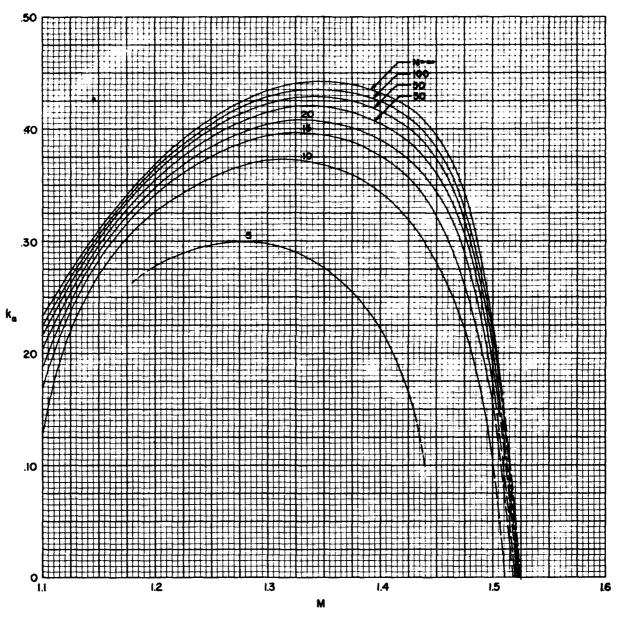


Figure 1201-5c STABILITY BOUNDARIES FOR SINGLE-DEGREE-OF-FREEDOM TORSIONAL FLUTTER FOR ZERO DAMPING (g $_{lpha}$ = 0). r = -0.4

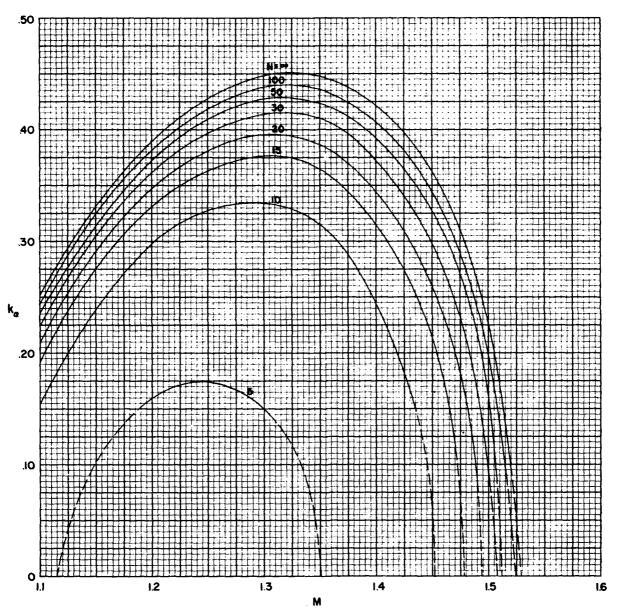


Figure 1201-5d STABILITY BOUNDARIES FOR SINGLE-DEGREE-OF-FREEDOM TORSIONAL FLUTTER FOR ZERO DAMPING (g $_{\alpha}$ = 0).

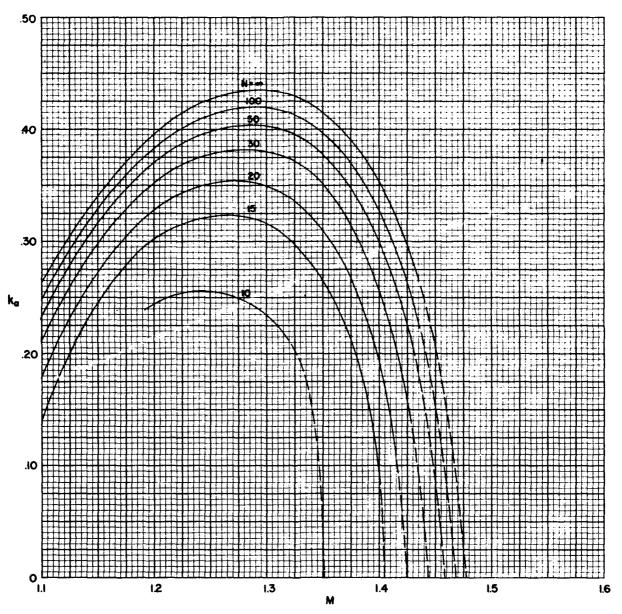


Figure 1201-5e STABILITY BOUNDARIES FOR SINGLE-DEGREE-OF-FREEDOM TORSIONAL FLUTTER FOR ZERO DAMPING (g $_{\alpha}$ = 0). r = -0.8

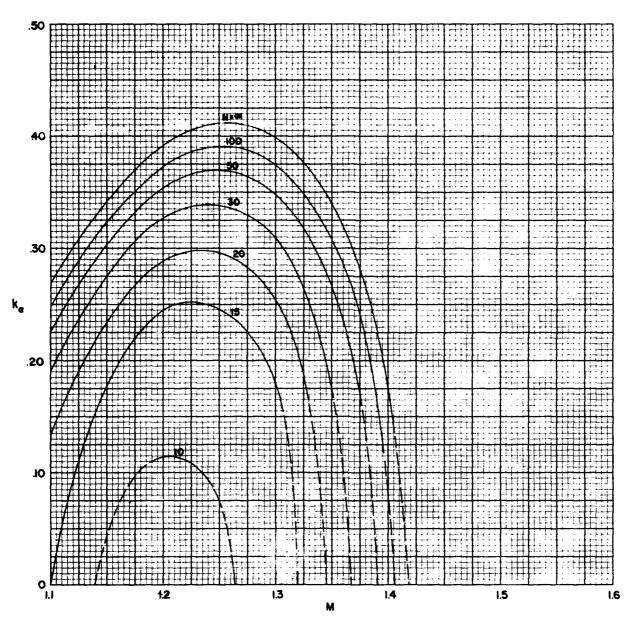


Figure 1201-5f STABILITY BOUNDARIES FOR SINGLE-DEGREE-OF-FREEDOM TORSIONAL FLUTTER FOR ZERO DAMPING (g $_{\alpha}$ = 0). r = -1.0

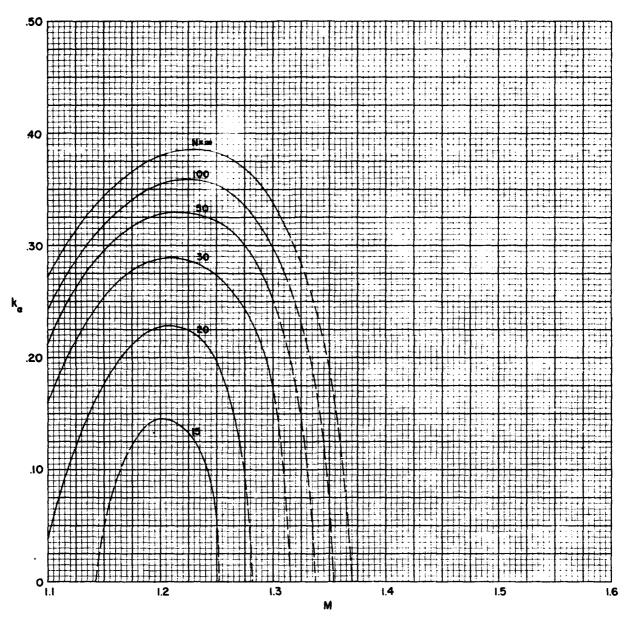


Figure 1201-5g STABILITY BOUNDARIES FOR SINGLE-DEGREE-OF-FREEDOM TORSIONAL FLUTTER FOR ZERO DAMPING (g $_{\alpha}$ = 0). r = -1.2

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1202 Two-Dimensional Binary Flexure-Torsion Flutter

The equations of motion for a two-dimensional airfoil in flexure and torsion are most easily derived (References 12-12 and 12-13) by use of the Lagrangian equations

$$\frac{d}{dt} \left(\frac{\partial E_k}{\partial \dot{q}_1} \right) + \frac{\partial E_e}{\partial q_1} + \frac{\partial F}{\partial \dot{q}_1} - L_g = 0$$

$$\frac{d}{dt} \left(\frac{\partial E_k}{\partial \dot{q}_2} \right) + \frac{\partial E_e}{\partial q_2} + \frac{\partial F}{\partial \dot{q}_2} - M_g = 0$$
(1202-1)

and

The quantities \mathbf{q}_1 and \mathbf{q}_2 are the generalized coordinates describing the motion of the system; they may be considered as the translational displacement h' of the wing elastic axis, and the angular displacement α , respectively, although this choice is not essential. Thus, for harmonic oscillatory motions we get:

$$h' = q_1 = h'_o e^{i\omega t}$$

$$\alpha = q_2 = \alpha_o e^{i\omega t}$$
(1202-2)

The quantities L_g and M_g are the generalized aerodynamic force and moment per unit span, respectively.

The kinetic energy $\mathbf{E}_{\mathbf{k}}$ of the system per unit span can be written as the sum of the translational and rotational energies about an axis through the center of gravity, as follows,

$$E_{k} = \frac{1}{2} m \left[h' + x_{\alpha} b \dot{\alpha} \right]^{2} + \frac{1}{2} \left[I'_{\alpha} - m (x_{\alpha} b)^{2} \right] \dot{\alpha}^{2}$$
 (1202-3)

Expanding, substituting S for the mass unbalance quantity mx_{α} b, and also writing the equations for the elastic energy \mathbf{E}_{e} and half the rate of energy dissipation F per unit span, one obtains:

$$E_{k} = \frac{1}{2} (m\dot{h}'^{2} + 2S\dot{h}'\dot{\alpha} + I'_{\alpha}\dot{\alpha}^{2})$$

$$E_{e} = \frac{1}{2} (C_{h}h'^{2} + C_{\alpha}\alpha^{2})$$

$$F = \frac{1}{2} \left(\frac{g_{h}C_{h}}{\omega} \dot{h}'^{2} + \frac{g_{\alpha}C_{\alpha}}{\omega} \dot{\alpha}^{2} \right)$$
(1202-4)

By introducing the generalized coordinates q_1 and q_2 (Equations 1202-2) into these energy equations, taking derivatives, and then substituting into the Lagrangian equations of motion (Equations 1202-1), we have:

$$-\omega^{2} m h_{o}^{'} e^{i\omega t} - \omega^{2} S \alpha_{o} e^{i\omega t} + C_{h} h_{o}^{'} e^{i\omega t} + i g_{h} C_{h} h_{o}^{'} e^{i\omega t} - L_{g} = 0$$

$$(1202-5)$$

$$-\omega^{2} I_{\alpha}^{'} \alpha_{o} e^{i\omega t} - \omega^{2} S h_{o}^{'} e^{i\omega t} + C_{\alpha} \alpha_{o} e^{i\omega t} + i g_{\alpha} C_{\alpha} \alpha_{o} e^{i\omega t} - M_{g} = 0$$

The generalized force and moment per unit span on a two-dimensional wing about the elastic axis (see Equations 1203-10) are:

$$L_{g} = L' = -\pi \rho b^{3} \omega^{2} e^{i\omega t} \left(A_{11} \frac{h'_{o}}{b} + A_{12} \alpha_{o} \right)$$

$$M_{g} = M' = -\pi \rho b^{4} \omega^{2} e^{i\omega t} \left(A_{21} \frac{h'_{o}}{b} + A_{22} \alpha_{o} \right)$$
(1202-6)

where (see Equations 1203-9)

$$A_{11} = C_{Lh}$$

$$A_{12} = C_{Lh} (\frac{1}{2} + r) - C_{L\alpha}$$

$$A_{21} = C_{Lh} (\frac{1}{2} + r) - C_{Mh}$$

$$A_{22} = -C_{M\alpha} - C_{Lh} (\frac{1}{2} + r)^2 + (C_{L\alpha} + C_{Mh}) (\frac{1}{2} + r)$$
(1202-7)

By combining Equations 1202-5 and 1202-6, and rearranging (since $\omega_{\rm h}=\sqrt{c_{\rm h}/m},~\omega_{\alpha}=\sqrt{c_{\alpha}/I_{\alpha}}$, and S = mx_{\alpha}b), we have:

$$\int_{1}^{\infty} \frac{m}{\pi \rho b^{2}} \left[\left(\frac{\omega_{h}}{\omega} \right)^{2} (1 + ig_{h}) - 1 \right] + A_{11} \right] \frac{h'_{o}}{b} + \left\{ -\frac{mx}{\pi \rho b^{2}} + A_{12} \right\} \alpha_{o} = 0$$

$$\left\{ -\frac{mx}{\pi \rho b^{2}} + A_{21} \right\} \frac{h'_{o}}{b} + \left\{ \frac{i'_{o}}{\pi \rho b^{4}} \left[\left(\frac{\omega_{o}}{\omega} \right)^{2} (1 + ig_{o}) - 1 \right] + A_{22} \right\} \alpha_{o} = 0$$

$$(1202-8)$$

In order for a solution to exist, the determinant of Equations 1202-8 must vanish. That is,

Where

$$M_{11} = \frac{m}{\pi \rho b^{2}} \left[\left(\frac{\omega_{h}}{\omega} \right)^{2} (1 + ig_{h}) - 1 \right]$$

$$M_{12} = M_{21} = -\frac{mx_{\alpha}}{\pi \rho b^{2}} \qquad (1202-10)$$

$$M_{22} = \frac{i'_{\alpha}}{\pi \rho b^{4}} \left[\left(\frac{\omega_{\alpha}}{\omega} \right)^{2} (1 + ig_{\alpha}) - 1 \right]$$

Some methods of solving the determinantal equation for two-dimensional binary flutter will be covered in Subsection 1204. The determinantal equations of motion derived here (Equations 1202-7, 1202-9 and 1202-10) are identical to those presented in Reference 12-14.

1203 Three-Dimensional Binary Flexure-Torsion Flutter

Let the quantities, h' and α , describing the motion of the three-dimensional (finite) wing referred to the elastic axis be defined by (cf. Equations 1202-2)

$$h' = \phi_1 q_1 = \phi_1 h'_0 e^{i\omega t}$$

$$\alpha = \phi_2 q_2 = \phi_2 \alpha_0 e^{i\omega t}$$
(1203-1)

where ϕ_1 and ϕ_2 are functions of the spanwise position, y. The quantities q_1 and q_2 are generalized coordinates; they may be considered respectively as the displacement of, and rotation at, the tip of the wing, although in any specific case some other quantity may be more convenient.

The kinetic energy $\mathbf{E}_{\mathbf{k}}$ in such a system may be found from the spanwise integration (cf. Equation 1202-4)

$$E_{k} = \frac{1}{2} \left[\int_{0}^{1} m\dot{h}^{2} dy + 2 \int_{0}^{1} S\dot{h}^{2} \dot{\alpha} dy + \int_{0}^{1} I_{\alpha}^{2} \dot{\alpha}^{2} dy \right]$$
 (1203-2a)

The elastic energy $\mathbf{E}_{\mathbf{e}}$ in such a system is

$$E_{e} = \frac{1}{2} \left[\int_{0}^{\frac{1}{2}} EI \left(\frac{\partial^{2} h'}{\partial y^{2}} \right)^{2} dy + \int_{0}^{\frac{1}{2}} GJ \left(\frac{\partial \alpha}{\partial y} \right)^{2} dy \right]$$
 (1203-2b)

One-half the rate of energy dissipation is

$$F = \frac{1}{2} \left[-\frac{g_h}{\omega} \int_0^{\frac{1}{4}} EI \left(\frac{\partial^2 \dot{h}}{\partial y^2} \right)^2 dy - \frac{g_{\alpha}}{\omega} \int_0^{\frac{1}{4}} GJ \left(\frac{\partial \dot{\alpha}}{\partial y} \right)^2 dy \right]$$
 (1203-2c)

Since h' and α have been defined in Equations 1203-1, derivatives necessary for substitution in Equations 1203-2 may be formed. After substitution we have:

$$E_{k} = \frac{1}{2} \left[\int_{0}^{1} m \phi_{1}^{2} dy + 2 \int_{0}^{1} S \phi_{1} \phi_{2} \dot{q}_{1} \dot{q}_{2} dy + \int_{0}^{1} I_{\alpha}' \phi_{2}^{2} \dot{q}_{2}^{2} dy \right]$$

$$E_{e} = \frac{1}{2} \left[\int_{0}^{1} E I q_{1}^{2} \left(\frac{d^{2} \phi_{1}}{dy^{2}} \right)^{2} dy + \int_{0}^{1} G J q_{2}^{2} \left(\frac{d \phi_{2}}{dy} \right)^{2} dy \right]$$

$$F = \frac{1}{2} \left[-\frac{g_{h}}{\omega} \int_{0}^{1} E I \dot{q}_{1}^{2} \left(\frac{d^{2} \phi_{1}}{dy^{2}} \right)^{2} dy - \frac{g_{\alpha}}{\omega} \int_{0}^{1} G J \dot{q}_{2}^{2} \left(\frac{d \phi_{2}}{dy} \right)^{2} dy \right]$$

$$(1203-3)$$

The Lagrangian equations of motion for such a system of two degrees of freedom are (cf. Equations 1202-1):

$$\frac{\mathrm{d}}{\mathrm{dt}} \left(\frac{\partial \mathbf{E}_{\mathbf{k}}}{\partial \dot{\mathbf{q}}_{1}} \right) + \frac{\partial \mathbf{E}_{\mathbf{e}}}{\partial \mathbf{q}_{1}} + \frac{\partial \mathbf{F}}{\partial \dot{\mathbf{q}}_{1}} - \mathbf{L}_{\mathbf{g}} = 0 \qquad (1203-4)$$

$$\frac{d}{dt} \left(\frac{\partial E_k}{\partial \dot{q}_2}\right) + \frac{\partial E_e}{\partial q_2} + \frac{\partial F}{\partial \dot{q}_2} - M_g = 0$$

where L_g and M_g are the generalized aerodynamic force and moment per unit span acting on the wing, referred to the generalized coordinates q_1 and q_2 , respectively. The former will be more fully defined in Equations 1203-7 and 1203-8, respectively.

Taking the necessary partial derivatives of the energy equations (1203-3) and substituting into the Lagrangian equations (1203-4), we have:

$$-\omega^{2}e^{i\omega t} h'_{o} \int_{0}^{1} m\phi_{1}^{2} dy - \omega^{2}e^{i\omega t} \alpha_{o} \int_{0}^{1} S \phi_{1} \phi_{2} dy + h'_{o}e^{i\omega t} \int_{0}^{1} EI \left(\frac{d^{2}\phi_{1}}{dy^{2}}\right)^{2} dy$$

$$+ ig_{h}h'_{o}e^{i\omega t} \int_{0}^{1} EI \left(\frac{d^{2}\phi_{1}}{dy^{2}}\right)^{2} dy - L_{g} = 0 \qquad (1203-5)$$

$$-\omega^{2}e^{i\omega t} h_{o}^{'} \int_{0}^{R} S \phi_{1} \phi_{2} dy - \omega^{2}e^{i\omega t} \alpha_{o} \int_{0}^{R} I_{\alpha}^{'} \phi_{2}^{2} dy + \alpha_{o}e^{i\omega t} \int_{0}^{R} GJ \left(\frac{d \phi_{2}}{dy}\right)^{2} dy$$

$$+ ig_{\alpha}\alpha_{o}e^{i\omega t} \int_{0}^{R} GJ \left(\frac{d \phi_{2}}{dy}\right)^{2} dy - M_{g} = 0 \qquad (1203-6)$$

Borbely's and Possio's equations for the lift and moment on a unit span of two-dimensional wing oscillating in flexure and torsion are derived in References 12-1 and 12-15, respectively, and are reproduced in Reference 12-14. Using the coefficients defined by Equations 1201-3, the force and moment about the elastic axis may be written, respectively:

$$L' = -\pi \rho b^{3} \omega^{2} e^{i\omega t} \left\{ -C_{Lh} \frac{h'_{o}}{b} + \left[(\frac{1}{2} + r) C_{Lh} - C_{L\alpha} \right] \alpha_{o} \right\}$$

$$M' = -\pi \rho b^{4} \omega^{2} e^{i\omega t} \left\{ \left[-C_{Mh} + (\frac{1}{2} + r) C_{Lh} \right] \frac{h'_{o}}{b} + \left[-C_{M\alpha} \right] \right\}$$

$$-C_{Lh} (\frac{1}{2} + r)^{2} + C_{L\alpha} (\frac{1}{2} + r) + C_{Mh} (\frac{1}{2} + r) \right\} \alpha_{o}$$

$$(1203-8)$$

(Note- This equation for M' is derived independently in Subsection 1201; see Equation 1201-5 and the note that follows it.)

For convenience, let

$$A_{11} = -C_{Lh}$$

$$A_{12} = C_{Lh} (\frac{1}{2} + r) - C_{L\alpha}$$

$$A_{21} = C_{Lh} (\frac{1}{2} + r) - C_{Mh}$$

$$A_{22} = -C_{M\alpha} - C_{Lh} (\frac{1}{2} + r)^2 + C_{L\alpha} (\frac{1}{2} + r) + C_{Mh} (\frac{1}{2} + r)$$
(1203-9)

den, for two-dimensional wings,

$$L' = -\pi \rho b^{3} \omega^{2} e^{i\omega t} \left(A_{11} \frac{h'_{o}}{b} + A_{12} \alpha_{o} \right)$$

$$M' = -\pi \rho b^{4} \omega^{2} e^{i\omega t} \left(A_{21} \frac{h'_{o}}{b} + A_{22} \alpha_{o} \right)$$
(1203-10)

For three-dimensional wings, taking into account the spanwise variations of displacement (cf. Equations 1202-2 and 1203-1), we have

$$L' = - \pi \rho b^{3} \omega^{2} e^{i\omega t} \left(A_{11} \frac{\phi_{1} h_{o}'}{b} + A_{12} \phi_{2} \alpha_{o} \right)$$

$$M' = - \pi \rho b^{4} \omega^{2} e^{i\omega t} \left(A_{21} \frac{\phi_{1} h_{o}'}{b} + A_{22} \phi_{2} \alpha_{o} \right)$$

$$(1203-11)$$

By the principle of virtual work, and by use of Equations 1203-1 and 1203-11, the generalized moments and forces may then be expressed as follows:

$$L_{g} = -\pi\rho\omega^{2}e^{i\omega t}\left[h'_{o}\int_{0}^{1}b^{2}A_{11}\phi_{1}^{2}dy + \alpha_{o}\int_{0}^{1}b^{3}A_{12}\phi_{1}\phi_{2}dy\right]$$

$$M_{g} = -\pi\rho\omega^{2}e^{i\omega t}\left[h'_{o}\int_{0}^{1}b^{3}A_{21}\phi_{1}\phi_{2}dy + \alpha_{o}\int_{0}^{1}b^{4}A_{22}\phi_{2}^{2}dy\right]$$
(1203-12)

These may be substituted into Equations 1203-5 and 1203-6, respectively, to obtain the equations of motion, thus:

$$(M'_{11} + A'_{11}) h'_{0} + (M'_{12} + A'_{12}) \alpha_{0} = 0$$

$$(M'_{21} + A'_{21}) h'_{0} + (M'_{22} + A'_{22}) \alpha_{0} = 0$$
(1203-13)

A necessary condition for the existence of a solution of these equations is

$$\begin{vmatrix}
M'_{11} + A'_{11} & M'_{12} + A'_{12} \\
M'_{21} + A'_{21} & M'_{22} + A'_{22}
\end{vmatrix} = 0$$
(1203-14)

where

$$\begin{split} \mathbf{M}_{11}' &= -\int_{0}^{1} m \phi_{1}^{2} \, \mathrm{d}y + \frac{1}{\omega^{2}} \, (1 + i \mathbf{g}_{h}) \int_{0}^{1} EI \left(\frac{\mathrm{d}^{2} \phi_{1}}{\mathrm{d}y^{2}}\right)^{2} \, \mathrm{d}y \\ \mathbf{M}_{12}' &= \mathbf{M}_{21}' = -\int_{0}^{1} S \phi_{1} \phi_{2} \, \mathrm{d}y \\ \mathbf{M}_{22}' &= -\int_{0}^{1} I_{\alpha}' \phi_{2}^{2} \, \mathrm{d}y + \frac{1}{\omega^{2}} \, (1 + i \mathbf{g}_{\alpha}) \int_{0}^{1} GJ \left(\frac{\mathrm{d} \phi_{2}}{\mathrm{d}y}\right)^{2} \, \mathrm{d}y \\ \mathbf{A}_{11}' &= \pi \rho \int_{0}^{1} b^{2} \mathbf{A}_{11} \phi_{1}^{2} \, \mathrm{d}y \\ \mathbf{A}_{21}' &= \pi \rho \int_{0}^{1} b^{3} \mathbf{A}_{21} \phi_{1} \phi_{2} \, \mathrm{d}y \\ \mathbf{A}_{22}' &= \pi \rho \int_{0}^{1} b^{4} \mathbf{A}_{22} \phi_{2}^{2} \, \mathrm{d}y \end{split}$$

$$(1203-15)$$

In general, for three-dimensional wings, each factor in every one of the foregoing integrands is a function of its spanwise location, for various reasons as indicated below:

Wing Characteristic Determining the

Spanwise Function	Determined Determined
Mass distribution	m, S, I'a
Material	E, G
Cross-section form	I, J
Planform	b
Planform and elastic axis location	A ₁₁ , A ₁₂ , A ₂₁ , A ₂₂
Mode shape in flexure	ϕ_{1}
Mode shape in torsion	ϕ_{2}

Ougntities Co

Further, it is seen that the quantities M_{11}' , M_{12}' , M_{21}' , and M_{22}' are functions of the mechanical parameters and frequency, but not of the flight conditions. However, the aerodynamic terms A_{11}' , A_{12}' , A_{21}' and A_{22}' , are functions of Mach number and the location of the elastic axis relative to the mid-chord line, as well as of the frequency and certain mechanical parameters.

For special cases, the above equations may be simplified to a large extent; for instance, a uniform rectangular cantilever wing would enable the computer to remove all terms other than ϕ_1 and ϕ_2 from the integrands.

Several methods of solving the determinantal equations (e.g. Equations 1202-9 and 1203-14) are possible. A method based on that of the U.S. Air Force Air Materiel Command (Reference 12-2) is presented as an example in Subsection 1204.

1204 Applications of Determinantal Equation for Two-Dimensional Binary Flutter

1204.0 Discussion

The determinantal equation for two-dimensional binary flutter (cf. Equation 1202-9) is

$$\begin{vmatrix}
M_{11} + A_{11} & M_{12} + A_{12} \\
M_{21} + A_{21} & M_{22} + A_{22}
\end{vmatrix} = 0 \qquad (1204.0-1)$$

where, (cf. Equations 1202-7 and 1202-10):

$$M_{11} = \frac{m}{\pi \rho b^{2}} \left[\left(\frac{\omega_{h}}{\omega} \right)^{2} \left(1 + i g_{h} \right) - 1 \right]$$

$$M_{12} = M_{21} = -\frac{m x_{\alpha}}{\pi \rho b^{2}}$$

$$M_{22} = \frac{I'_{\alpha}}{\pi \rho b^{4}} \left[\left(\frac{\omega_{\alpha}}{\omega} \right)^{2} \left(1 + i g_{\alpha} \right) - 1 \right] \qquad (1204.0-2)$$

$$A_{11} = -C_{Lh}$$

$$A_{12} = C_{Lh} \left(\frac{1}{2} + r \right) - C_{L\alpha}$$

$$A_{21} = C_{Lh} \left(\frac{1}{2} + r \right) - C_{Mh}$$

$$A_{22} = -C_{M\alpha} - C_{Lh} \left(\frac{1}{2} + r \right)^{2} + \left(C_{L\alpha} + C_{Mh} \right) \left(\frac{1}{2} + r \right)$$

A number of fairly simple solutions to the foregoing determinantal equation have been obtained, and one of these is outlined in the following subsection.

1204.1 Materiel Center Method (Peferences 12-2 and 12-16)

Let
$$g_{\alpha} = g_{h} = g$$

$$Z = \left(\frac{\omega_{\alpha}}{\omega}\right)^{2} \qquad (1204.1-1)$$

$$\Lambda = Z(1 + ig)$$
and
$$k_{h\alpha} = \left(\frac{\omega_{h}}{\omega_{\alpha}}\right)^{2}$$
Then
$$M_{11} = \frac{m}{\pi \rho b^{2}} \left(k_{h\alpha} \dot{\Lambda} - 1\right)$$

$$M_{22} = \frac{I'_{\alpha}}{\pi a b^{4}} \left(\Lambda - 1\right)$$

The determinantal equation may therefore be written

$$\Lambda^2 + C_1 \Lambda + C_2 = 0 \tag{1204.1-3}$$

where C_1 and C_2 are complex constants.

The two complex roots of this quadratic equation are given by

$$\Lambda = \frac{-c_1 + \sqrt{c_1^2 - 4c_2}}{2}$$
 (1204.1-4)

By complex algebra it is readily shown that

$$\sqrt{c_1^2 - 4c_2} = \sqrt[4]{\zeta^2 + \eta^2} \left(\cos\frac{\theta}{2} + i \sin\frac{\theta}{2}\right)$$
 (1204.1-5)

where

$$\zeta = (c_1^2 - 4c_2)$$

$$\eta = (c_1^2 - 4c_2)^*$$

$$\theta = arc \tan \frac{\eta}{\zeta}$$

Hence we may write the real and complex parts of the two roots of Equation 1204.1-4 as follows:

$$2\bar{\Lambda}_{1} = -\bar{C}_{1} + \sqrt[4]{\zeta^{2} + \eta^{2}} \cos \frac{\theta}{2}$$

$$2\bar{\Lambda}_{2} = -\bar{C}_{1} - \sqrt[4]{\zeta^{2} + \eta^{2}} \cos \frac{\theta}{2}$$

$$2\Lambda_{1}^{*} = -C_{1}^{*} + \sqrt[4]{\zeta^{2} + \eta^{2}} \sin \frac{\theta}{2}$$

$$2\Lambda_{2}^{*} = -C_{1}^{*} - \sqrt[4]{\zeta^{2} + \eta^{2}} \sin \frac{\theta}{2}$$

$$(1204.1-6)$$

$$2\Lambda_{2}^{*} = -C_{1}^{*} - \sqrt{\zeta^{2} + \eta^{2}} \sin \frac{\theta}{2}$$

By the definitions of Equations 1204.1-1 it is apparent that

$$\left(\frac{\omega_{\alpha} \mathbf{1}}{\omega}\right)^{2} = \overline{\Lambda}_{1}$$

$$\left(\frac{\omega_{\alpha} \mathbf{2}}{\omega}\right)^{2} = \overline{\Lambda}_{2}$$
(1204.1-7)

and since ω must be assumed in order for values of the aerodynamic coefficients to be chosen, then the values of ω are determined for this value of ω and for the simultaneously assumed value of Mach number M.

It is also apparent by the definitions of Equations 1204.1-1 that the damping coefficients are:

$$g_1 = \frac{\Lambda_1^*}{\overline{\Lambda}_1}$$

$$g_2 = \frac{\Lambda_2^*}{\overline{\Lambda}_2}$$
(1204.1-8)

Thus, the procedure for determining the stability of the wing at a given Mach number consists of:

- (a) Assuming a series of values for the reduced frequency k, thereby determining the values of the frequency parameter—and of the aerodynamic coefficients which will be used in the determinantal equation; then using these coefficients in solving the determinantal equation for the natural frequency in torsion and for the damping factor.
- (b) Plotting these computed damping factors against some convenient parameter such as ω_{α} or $\omega_{\alpha}b/a$.
- (c) Determining experimentally, or estimating from experience, the actual damping factors of the wing; and plotting this factor on the graph referred to in (b).

If, at a particular value of Mach number and natural frequency ω_{α} , the actual damping factor of the wing is greater than the computed value (i.e., if the point representing the experimental value lies above the curve representing the computed values) then freedom from flutter is indicated.

1204.11 Numerical Example by the Materiel Center Method

Let the following values be assumed to define the characteristics of a two-dimensional wing that is to be examined for binary flutter:

$$\frac{m}{\pi \rho b^2} = 100.0$$

$$\frac{I'_{\alpha}}{\pi \rho b^4} = 16.67$$

$$\frac{\omega_h}{\omega_{\alpha}} = 0.700$$

$$r = 0$$

$$x_{\alpha} = 0$$
(1204.11-1)

These values, when substituted in the M-terms (Equations 1204.0-2) of the determinantal equation give:

$$M_{11} = 100.0 (0.4900 \Lambda - 1)$$
 $M_{12} = M_{21} = 0$ (1204.11-2)

$$M_{22} = 16.67 (\Lambda - 1)$$

Let the flight Mach number (M) of interest be 1.4; and let the frequency range of interest be defined by a range from 0.2 to 0.7 for the frequency parameter Ω . For this immediate part of the numerical example the value 0.4 is chosen for the latter quantity.

That is

$$M = 1.4$$

$$\Omega = 0.4$$
(1204.11-3)

These two values determine the aerodynamic coefficients (as tabulated in Table 1208.2) to be:

$$C_{Lh}$$
 = -1.31345 - i 12.999891
 $C_{L\alpha}$ = -132.93679 - i 6.776163 (1204.11-4)
 C_{Mh} = -1.08389 - i 6.367874
 $C_{M\alpha}$ = -65.34705 + i 3.340791

For r = 0 and for these coefficients, the A-terms (Equation 1204.0-2) of the determinantal equation become:

$$A_{11} = 1.313 + i 13.000$$
 $A_{12} = 132.280 - i 13.276$ (1204.11-5)

 $A_{21} = 0.427 - i 0.132$
 $A_{22} = -1.335 + i 0.113$

Substituting these values for the M-terms (Equation 1204.11-2) and the A-terms (Equations 1204.11-5) into the determinantal equation 1204.0-1, we get:

$$\begin{vmatrix} 49.00 & \Lambda - 98.69 + i & 13.00 & 132.28 - i & 13.28 \\ 0.4272 - i & 0.1321 & 16.67 & \Lambda - 18.00 + i & 0.1133 \end{vmatrix} = 0$$
(1204.11-6)

This equation when expanded and simplified gives

$$\Lambda^2$$
 + (-3.094 + i 0.2721) Λ + (2.106 - i 0.2719) = 0 (1204.11-7)

By comparison of this equation with Equation 1204.1-3 it is apparent that the complex constants are:

$$C_1 = -3.094 + i 0.2721$$
 $C_2 = 2.106 - i 0.2719$
(1204.11-8)

The quantities that appear in the roots of the determinantal equation can be calculated by Equations 1204.1-5 as follows:

$$c_1^2 = 9.4994 - i \ 1.6838$$

$$4 c_2 = 8.4258 - i \ 1.0876$$

$$c_1^2 - 4 c_2 = 1.0735 - i \ 0.5962$$

$$\zeta = 1.0735$$

$$\eta = -0.5962$$

$$\sqrt[4]{\zeta^2 + \eta^2} = 1.1081$$

$$\theta = -29^{\circ} \ 2.74'$$

The real and imaginary parts of the two roots of the quadratic equation are therefore, by use of Equations 1204.1-6:

By Equations 1204.1-7 it is apparent that the natural frequencies of the wings (ω_{α}) in relation to the circular frequency (ω) corresponding to the specified Mach number and frequency parameter are given by:

$$\frac{\omega_{\alpha 1}}{\omega} = 1.443$$

$$\frac{\omega_{\alpha 2}}{\omega} = 1.005$$
(1204.11-11)

A convenient non-dimensional parameter for the natural frequency is ω_N b/a; this can be derived from the foregoing ratio by the identity

$$\frac{\omega_{\alpha}}{a} = \frac{\omega_{\alpha}}{\omega} \cdot \frac{\omega b}{V} \cdot \frac{V}{a}$$

where $\omega b/V$ (the reduced frequency k) is related to Mach number M and frequency parameter Ω as indicated in the list of symbols and in Table 1208.1.

For this numerical example we therefore find that

$$\frac{\omega b}{V} = 0.09796$$

$$\frac{v}{c} = 1.4$$
(1204.11-12)

and

Therefore,

$$\frac{\omega_{\alpha} 1^{b}}{a} = 0.1980$$

$$\frac{\omega_{\alpha} 2^{b}}{a} = 0.1379$$
(1204.11-13)

By Equations 1204.1-8 it is apparent that the damping coefficients corresponding to the two roots of the flutter equation are:

$$g_1 = -0.1320$$

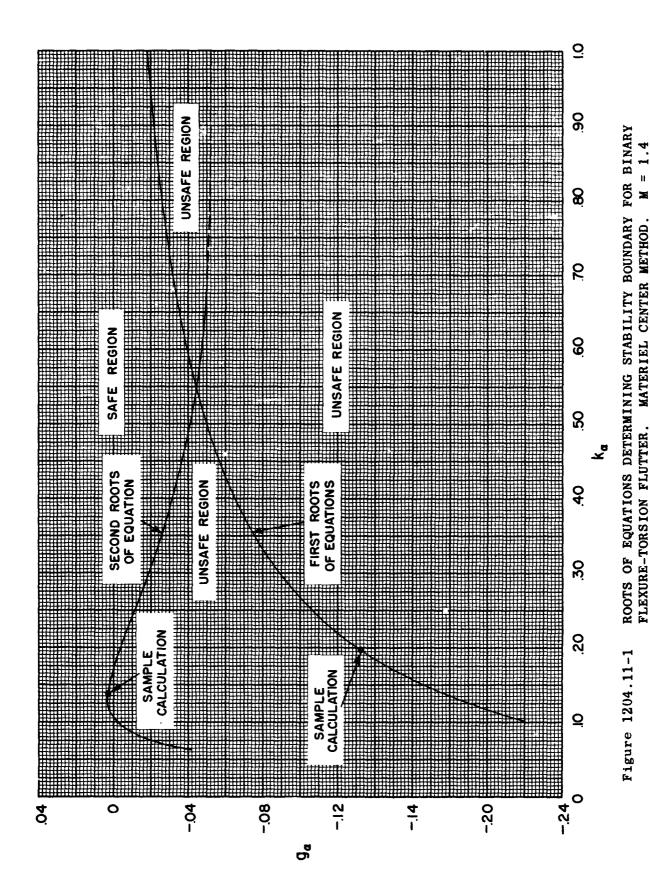
 $g_2 = +0.0029$ (1204.11-14)

Similar computations of $\omega_{\alpha} b/a$ (the reduced natural frequency k_{α}), and of g, have been computed for Ω = 0.2, 0.25, 0.3, 0.5, 0.6, 0.7, and 1.0 and then all of these values have been plotted (g vs k_{α}) in Figure 1204.11-1, for Mach number 1.4. In an actual investigation of the flutter characteristics of a wing similar computations and graphs would be computed for each of several other Mach numbers.

The actual value of the quantity k_{α} for the sample wing may be determined by experiment or estimated from experience. In the former case the natural frequency in torsion of the wing (ω_{α} in radians per second) would be measured, and also an average or effective semi-chord length of the wing would be determined. In addition, for each altitude of interest a value for the velocity of sound would be determined corresponding to the ambient temperature and composition of the air at that level.

Likewise the actual value of the damping factor of the wing in torsion would be determined by measuring the rate of decay of a damped torsional vibration of the wing structure, or by measuring the power required to sustain such a vibration at constant amplitude – or an estimate could be made of the torsional damping factor from past experiences. A similar determination would be made of the flexural damping factor of the wing structure, and both of these damping factors would be used in selecting a suitable common damping factor for the wing being considered.

The point representing the value of the damping factor (g) and of the non-dimensional parameter for the reduced natural frequency (\mathbf{k}_{α}) of the wing at a given altitude would then be plotted on the previously computed graphs such as represented in Figure 1204.11-1 for each Mach number of interest. If the point for the experimental quantities lies above both curves representing the two roots of the equation it is concluded that flutter is improbable. For example, if the quantity \mathbf{k}_{α} for the wing at sea level is 0.2527 and the smaller of the two damping factors is 0.0032 it is seen that the point representing this wing on the graph of Figure 1204.11-1, for M = 1.4 lies above both curves and therefore the wing appears to be free from flutter at this Mach number. Similar spotting of the experimental values on the graphs for other Mach numbers would be made to determine the possibility of flutter occurring at each of these Mach numbers.



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1205 Three-Dimensional Ternary Flexure-Flexure-Torsion Flutter (References 12-12 and 12-13)

In many cases of three-dimensional systems it will be found that the natural frequency in bending in the second mode may be nearly equal to the natural frequency in torsion. If this is found to be true, then it may be expected that the second bending mode will affect the flutter characteristics. In order to include the effects of the additional bending mode, let:

$$h = h_{1} + h_{2}$$

$$h_{1} = \phi_{1}(y)q_{1}(t) = \phi_{1}h_{10}e^{i\omega t}$$

$$h_{2} = \phi_{2}(y)q_{2}(t) = \phi_{2}h_{20}e^{i\omega t}$$

$$\alpha = \phi_{3}(y)q_{3}(t) = \phi_{3}\alpha_{0}e^{i\omega t}$$
(1205-1)

The process of determining the kinetic and elastic energies of the system, taking appropriate derivatives and substituting in the Lagrangian equations of motion, can be followed as in Subsection 1203. If this is done, the condition that the equations of motion have a solution will be

$$\begin{vmatrix} M_{11}^{"} + A_{11}^{"} & M_{12}^{"} + A_{12}^{"} & M_{13}^{"} + A_{13}^{"} \\ M_{21}^{"} + A_{21}^{"} & M_{22}^{"} + A_{22}^{"} & M_{23}^{"} + A_{23}^{"} \\ M_{31}^{"} + A_{31}^{"} & M_{32}^{"} + A_{32}^{"} & M_{33}^{"} + A_{33}^{"} \end{vmatrix} = 0$$
 (1205-2)

where

$$\begin{split} \mathbf{M}_{11}^{"} &= \int_{0}^{\frac{1}{2}} m \phi_{1}^{2} \left[\left(\frac{\omega_{h1}}{\omega} \right)^{2} (1 + i \mathbf{g}_{h1}) - 1 \right] dy \\ \mathbf{M}_{12}^{"} &= \mathbf{M}_{21}^{"} = -\int_{0}^{\frac{1}{2}} m \phi_{1} \phi_{2} dy = 0 \text{ (by orthogonality)} \\ \mathbf{M}_{13}^{"} &= \mathbf{M}_{31}^{"} = -\int_{0}^{\frac{1}{2}} \mathbf{S} \phi_{1} \phi_{3} dy \\ \mathbf{M}_{22}^{"} &= \int_{0}^{\frac{1}{2}} m \phi_{2}^{2} \left[\left(\frac{\omega_{h2}}{\omega} \right)^{2} (1 + i \mathbf{g}_{h2}) - 1 \right] dy \\ \mathbf{M}_{23}^{"} &= \mathbf{M}_{32}^{"} = -\int_{0}^{\frac{1}{2}} \mathbf{S} \phi_{2} \phi_{3} dy \\ \mathbf{M}_{33}^{"} &= \int_{0}^{\frac{1}{2}} I_{\alpha} \phi_{3}^{2} \left[\left(\frac{\omega_{\alpha}}{\omega} \right)^{2} (1 + i \mathbf{g}_{\alpha}) - 1 \right] dy \end{split}$$

$$A_{11}^{"} = \pi \rho \int_{0}^{4} b^{2} A_{11} \phi_{1}^{2} dy$$

$$A_{12}^{"} = A_{21}^{"} = \pi \rho \int_{0}^{4} b^{2} A_{11} \phi_{1} \phi_{2} dy$$

$$A_{13}^{"} = \pi \rho \int_{0}^{4} b^{3} A_{12} \phi_{1} \phi_{2} dy$$

$$A_{22}^{"} = \pi \rho \int_{0}^{4} b^{2} A_{11} \phi_{2}^{2} dy$$

$$A_{31}^{"} = \pi \rho \int_{0}^{4} b^{3} A_{12} \phi_{2} \phi_{3} dy$$

$$A_{32}^{"} = \pi \rho \int_{0}^{4} b^{3} A_{21} \phi_{1} \phi_{3} dy$$

$$A_{33}^{"} = \pi \rho \int_{0}^{4} b^{4} A_{22} \phi_{3}^{2} dy$$

$$A_{33}^{"} = \pi \rho \int_{0}^{4} b^{4} A_{22} \phi_{3}^{2} dy$$

The values of the unprimed A_{11} , A_{12} , A_{21} , A_{22} are the same as in Subsection 1202 (Equation 1202-7). The method of solving Equation 1205-2 will be discussed in Subsection 1207. An application of this general method to subsonic flutter is given in References 12-12 and 12-13.

1206 Two-Dimensional Ternary Flexure-Torsion-Aileron Flutter

The determinantal equation for two-dimensional ternary bending-torsion-aileron flutter may be written, corresponding to that for binary flutter (Equation 1202-9), as

$$\begin{vmatrix}
M_{11} & + & A_{11} & M_{12} & + & A_{12} & M_{13} & + & A_{13} \\
M_{21} & + & A_{21} & M_{22} & + & A_{22} & M_{23} & + & A_{23} \\
M_{31} & + & A_{31} & M_{32} & + & A_{32} & M_{33} & + & A_{33}
\end{vmatrix} = 0 \qquad (1206-1)$$

where M_{11} M_{22} and A_{11} A_{22} are exactly as defined in Subsection 1202. These are repeated here for convenience. In addition, the forces and moments about the elastic axis due to the motion of the aileron, and the moments about the aileron hinge line also are given here. Thus,

$$\begin{split} \mathbf{M}_{11} &= \frac{m}{\pi \rho \mathbf{b}^2} \left[\left(\frac{\omega_{\mathbf{h}}}{\omega} \right)^2 (1 + i \mathbf{g}_{\mathbf{h}}) - 1 \right] \\ \mathbf{M}_{12} &= \mathbf{M}_{21} = -\frac{m \mathbf{x}_{\alpha}}{\pi \rho \mathbf{b}^2} \\ \mathbf{M}_{22} &= \frac{\mathbf{I}_{\alpha}}{\pi \rho \mathbf{b}^4} \left[\left(\frac{\omega_{\alpha}}{\omega} \right)^2 (1 + i \mathbf{g}_{\alpha}) - 1 \right] \\ \mathbf{M}_{13} &= \mathbf{M}_{31} = -\frac{m_{\beta} \mathbf{x}_{\beta}}{\pi \rho \mathbf{b}^2} \\ \mathbf{M}_{23} &= \mathbf{M}_{32} = -\frac{\mathbf{I}_{\beta}}{\pi \rho \mathbf{b}^4} - \frac{m_{\beta}}{\pi \rho \mathbf{b}^2} (\mathbf{c} - \mathbf{r}) \mathbf{x}_{\beta} \\ \mathbf{M}_{33} &= \frac{\mathbf{I}_{\beta}}{\pi \rho \mathbf{b}^4} \left[\left(\frac{\omega_{\beta}}{\omega} \right)^2 (1 + i \mathbf{g}_{\beta}) - 1 \right] \end{split}$$

The aerodynamic coefficients not involving the aileron are identically as given in Equations 1202-7, that is:

$$A_{11} = -C_{Lh}$$

$$A_{12} = C_{Lh} (\frac{1}{2} + r) - C_{L\alpha}$$

$$A_{21} = C_{Lh} (\frac{1}{2} + r) - C_{Mh}$$

$$A_{22} = -C_{M\alpha} - C_{Lh} (\frac{1}{2} + r)^2 + (C_{L\alpha} + C_{Mh}) (\frac{1}{2} + r)$$

The aerodynamic terms involving the aileron are:

$$A_{13} = -\left(\frac{1-c}{2}\right)^3 \left(\frac{1}{2} C'_{Lh} + C'_{L\alpha}\right)$$

$$\mathbf{A_{23}} = -\left(\frac{1-c}{2}\right)^{4} \left[\mathbf{C_{M\alpha}'} + \mathbf{C_{Lh}'} \left(\frac{\mathbf{c} - \mathbf{r}}{1-\mathbf{c}} + \frac{1}{4} \right) + \mathbf{C_{L\alpha}'} \left(2 \frac{\mathbf{c} - \mathbf{r}}{1-\mathbf{c}} + \frac{1}{2} \right) + \frac{1}{2} \mathbf{C_{Mh}'} \right]$$

$$A_{31} = C_{Lh} \left(\frac{1}{2} + c\right) - C_{Mh} - \left(\frac{1+c}{2}\right)^4 \left(\frac{3}{2} C_{Lh}^{"} - C_{Mh}^{"}\right)$$
 (1206-4)

$$\begin{split} &A_{32} = - \ C_{M\alpha} - \ C_{Lh} \ (\frac{1}{2} + \ r) \ (\frac{1}{2} + \ c) \ + \ C_{L\alpha} \ (\frac{1}{2} + \ c) \ + \ C_{Mh} \ (\frac{1}{2} + \ r) \\ &- (\frac{1 + c}{2})^4 \ \left[- \ C_{M\alpha}^{"} - \frac{3}{2} \ C_{Lh}^{"} \ \left(2 \ \frac{r + 1}{c + 1} \ - \frac{1}{2} \right) + C_{L\alpha}^{"} \ \left(2 \ \frac{r + 1}{c + 1} \ - \frac{1}{2} \right) \ + \frac{3}{2} \ C_{Lh}^{"} \right] \end{split}$$

$$A_{33} = -\left(\frac{1-c}{2}\right)^4 \left(C'_{M\alpha} + \frac{1}{4} C'_{Lh} + \frac{1}{2} C'_{L\alpha} + \frac{1}{2} C'_{Mh}\right)$$

All of the aerodynamic flutter coefficients (i.e., all of the C, C' and C' coefficients) are obtained from Table 1208-2, in which values of the coefficients are tabulated with Mach number (M) and the frequency parameter (Ω) as independent parameters, where the latter is a function of M, V, ω , and b (see the symbols list). In the case of the C-coefficients, b is the semi-chord of the entire wing; for the C'-coefficients, b is the semi-chord of the aileron; and for the C''-coefficients, b is the semi-chord of that portion of the wing forward of the aileron. For any given wing-aileron combination it is assumed for flutter analyses that the circular frequency ω is the same for all primed or umprimed C-coefficients.

It should be noted that if the aileron flutter alone (with no wingtorsion or bending) is being investigated, the two families of curves in Figures 1201-4 and 1201-5 apply, if the aileron is assumed to be hinged at the leading edge (i.e., r = -1.0).

Solution of Higher Order (above second order) Determinantal Flutter Equations

If, in the ternary flutter determinantal equations of motion (e.g., Equations 1205-2 and 1206-1), it is assumed that the frequencies bear a fixed ratio to each other, and that structural damping factors are equal, we may write:

$$z = \left(\frac{\omega_{\alpha}}{\omega}\right)^{2}$$

$$g = g_{h} = g_{\alpha} = g_{\beta}$$

$$\Lambda = z (1 + ig)$$
(1207-1)

It is then found that the ternary determinantal equations may be put in the form of a third degree polynomial such as

$$\Delta_0 \Lambda^3 + \Delta_1 \Lambda^2 + \Delta_2 \Lambda + \Delta_3 = 0$$
 (1207-2)

Since, in supersonic flutter analyses it is necessary to solve the determinantal equation for each Mach number of interest, it is obvious that considerable computational work is required. Three methods of solving these higher-order flutter equations (including quadric as well as cubic equations) have been investigated by Ruggiero and recorded in Reference 12-17.

As an alternative to solving the cubic equation, one may assume that the bending and aileron frequencies are fixed quantities instead of being in fixed ratios with the torsional frequency. Then, on expanding the determinant, the stability equation will be linear in Λ and the torsional frequency may be found directly. After plotting ω_{α} and g_{α} versus 1/k or some other parameter, it will be found that at some value of k the calculated ω_{α} will be the same as the actual natural frequency. Thus, the torsional damping factor found at that value of k will determine the stability of the system.

Other modifications of the method may be made, for instance: (1) assume the aileron natural frequency known, and the value of \mathbf{k}_α known, and then solve the resulting quadratic in Λ ; (2) assume that the damping is zero, the aileron natural frequency known, and then solve for Z and \mathbf{k}_α . These methods may also be applied in principle to the binary equations discussed in Subsection 1204.

1208 Tables

1208.1 Reduced Frequency (k); Mach Number (M) and Frequency

Parameter (Q) Independent

1.1 1.2 1.3 1.4 0008678 .001528 .002041 .002449 001736 .004583 .004683 .004898 002471 .005111 .008166 .004898 0052471 .005112 .005124 .004594 0055077 .005128 .005166 .004796 005678 .01528 .0153 .01469 01736 .01528 .02041 .0249 01736 .02529 .02041 .0249 01736 .02529 .03062 .0488 02169 .02041 .0249 .0488 02169 .02041 .0249 .0488 02169 .05104 .06122 .0488 02169 .05104 .06122 .05104 02169 .05104 .06122 .05104 02507 .05147 .07145 .0789 05207 .09167 .1225 .1459 06074 .1069 .1724 .1659 06942 .1222 .1628 .1714 06943<
200 400 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0

Table 1208.1 REDUCED FREQUENCY (k); MACH NUMBER (M) AND FREQUENCY PARAMETER (A) INDEPENDENT

	22							
2.4	. 00413 . 01240 . 01653 . 01653	. 05306 . 04133 . 06193 . 08264 . 1033			. 5785 . 4511 . 8264 . 9090	1.0743 1.1569 1.2396 1.462	1. 650 1. 0650 1. 0650 1. 0650 1. 0650 1. 0650 1. 0650	6. 1979 6. 2639
2. 2	. 003967 . 007934 . 01190 . 01587	. 03967 . 05950 . 07934 . 09917	11190 115838 21983 2883 8083	. 1177 . 1174 . 1570 . 4760		1.058 1.1058 1.1104 1.1901 1.001		5. 9504
2.0	. 003750 . 007500 . 01125 . 01500	. 08000 . 08150 . 07500 . 08150	1112 15512 18500 1855 1855			. 9750 1, 9750 1, 1250 1, 3125	1. 5000 1. 5000 1. 5000 1. 5000 1. 5000 1. 5000	5. 62 50 7. 5 000
1.9	. 003615 . 007230 . 01084 . 01446 . 02169	01892 05615 05412 07130	. 1265 . 1265 . 1867 . 2169	, , , , , , , , , , , , , , , , , , ,	. 5061 6504 7230 7953	. 8676 . 9399 1. 0122 1. 0845 1. 2652	1. 4460 1. 6267 1. 8075 3. 7112 3. 6150	5. 4224 7. 2399
1.8	. 003457 . 006914 . 01037 . 01383	. 02765 . 052857 . 069185 . 06614	1087 11880 17883 2074	242 2136 2136 2136 2136 2136 2136 2136 213	4840 6233 6614 7605	. 8988 . 8988 . 9679 1. 0870 1. 2099	1. 55527 1. 5555 2. 5526 3. 4566	5. 1852 6. 9136
1.7	. 003270 . 006540 . 009810 . 01308	. 02616 . 04805 . 06540 . 08175	. 09810 . 1144 . 1536 . 1635		. 5548 6588 6588 6540 710	. 7848 . 9156 . 9810 1. 1445	1. 4080 2. 4535 3. 4534 3. 4534	4. 9048 6. 5398
* \0	28828	80208	88488 88600		4000M	46 000	440,00	15.0 20.0

Table 1208.1 REDUCED FREQUENCY (k); MACH NUMBER (M)
AND FREQUENCY PARAMETER (G) INDEPENDENT (Continued)

=	. i	æ	9.0	e .	3.4	3.6
	. 004160 . 008511 . 01178 . 01704	. 004562 . 008724 . 01309 . 01745	. 004444 . 006889 . 01333 . 01778	. 004512 . 009023 . 01854 . 01805	. 004567 . 009135 . 01370 . 01827	. 004614 . 009228 . 01384 . 02769
	. 0344 0446 06446 08521 108521	. 05545 . 06543 . 0674 . 1091	. 03556 . 0444 . 06667 . 1111	. 03609 . 04512 . 06768 . 1128	. 03654 . 04567 . 06851 . 08135	04691 04614 06921 1154
	21.1.1.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.	1500 1745 1745 1881 161	2112 2112 2112 212 213 213 213 213 213 2	11355 11555 11855 12856 107	113 113 128 128 140 140	1384 1615 1846 2307
				. 3158 . 3609 . 4512 . 5414	. 3197 . 3197 . 4511 . 5567	3830 4153 5584 5584
 	. 5964 . 6854 . 8589 . 8589	. 6107 . 6980 . 8785 . 8784 . 7852	. 6222 . 7111 . 8000 . 8889 . 9778	. 42119 . 90231 . 9023	. 6394 . 7308 . 8221 . 9135 1. 0048	. 6460 . 7383 . 8306 . 9228 1. 0151
	1.0225 1.1027 1.1929 1.2781 1.4911	1.0469 1.1342 1.3214 1.5268	1.1.1.06 1.1.2.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1	1. 0828 1. 1630 1. 2633 1. 3535 1. 5791	1. 0962 1. 1875 1. 3702 1. 5986	1.1074 1.1997 1.2920 1.3843 1.6150
	1. 7041 2. 1302 3. 1853 4. 2604	1. 7449 2. 1811 3. 2711 4. 3711	1. 4044 6. 6838 6. 6838 6. 6444	1. 8047 2. 08047 3. 2858 4. 51117	2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.	1, 8457 2, 0764 3, 3071 4, 6142
	6. 3905 8. 5207	6. 5434 6. 7245	6. 6667 8. 8889	6.7676 9.0234	6.8512 9.1349	6. 9213 9. 2284

Table 1208.1 REDUCED FREQUENCY (k); MACH NUMBER (M)
AND FREQUENCY PARAMETER (Q) INDEPENDENT (Continued)

7.0	. 004898 . 009796 . 01469 . 01959	. 05918 . 04898 . 09747 . 1224	1714 1959 2449 2939		. 6857 . 7837 . 8816 . 9796 1. 0776	1. 1755 1. 2735 1. 4694 1. 4694	1.9592 2.2041 3.6735 4.8980	7.3469 9.7959
6.0	. 004861 . 099722 . 01458 . 01944	. 03889 . 04861 . 07292 . 1215	. 1458 . 1944 . 2431 . 2917		. 6806 . 7778 . 8750 . 9722 1. 0694	1. 1667 1. 2639 1. 4583 1. 7014	1. 9444 2. 1875 3. 6458 4. 8611	7. 2917 9. 7222
5.0	. 004800 . 009600 . 01440 . 01920 . 02880	. 03840 . 04800 . 07200 . 1200	. 1440 . 1920 . 2400	3360 - 4320 - 4800 5760	. 6720 . 7680 . 8640 . 9600 1. 0560	1. 1520 1. 2480 1. 3440 1. 6800	1. 9200 2. 1600 3. 6000 4. 8000	7. 2000 9. 6000
4.5	. 004753 . 009506 . 01426 . 01901 . 02852	. 03802 . 04753 . 07130 . 08506	. 1426 . 1964 . 2377 . 2852	3327 4278 4753 5704	.6654 .7605 .8556 .0457	1. 2358 1. 3358 1. 4259 1. 6636	1.9012 2.1389 3.5648 4.7531	7.1296 9.5062
4.0	. 004688 . 009375 . 01406 . 01875	. 03750 . 04688 . 07031 . 09375	. 1406 . 1841 . 2344 . 2812	. 3281 . 4219 . 4688 . 5625	. 6562 . 7500 . 9438 . 9375	1. 1250 1. 2188 1. 3125 1. 4062 1. 6406	1.8750 2.1094 2.3438 3.5156 4.6875	7.0312 9.3750
S. 8	. 004654 . 009307 . 01396 . 01861	03723 26584 09897 168	. 1596 . 1861 . 2321 . 2321		6515 3446 8377 9307 1.0238	1. 2169 1. 2100 1. 3951 1. 6288	1. 8615 2. 3269 3. 4903 6537	6. 9806 9. 3075
*	25328	20202 20202 20202	86556 6656 6656 6656 6656 6656 6656 665	1.0000		, , , , , , , , , , , , , , , , , , ,	44.0.6.0 0 0 0 0 0	15.0 20.0

Table 1208.1 REDUCED FREQUENCY (k); MACH NUMBER (M)
AND FREQUENCY PARAMETER (\(\Omega\) INDEPENDENT (Continued)

12.0	. 004965 . 009931 . 01490 . 01986	. 03972 . 04965 . 07448 . 09931	. 1490 . 1738 . 1986 . 2483	344 3944 4469 59865 59865	6951 7944 8938 9931 1.0924	1. 1917 1. 2910 1. 3903 1. 4896 1. 7378	1,9861 22,2344 3,4826 4,9826 653	7. 4479 9. 9306
11.0	. 004959 . 009917 . 01488 . 01983	. 03967 . 04959 . 07438 . 09917 . 1240	. 1488 . 1736 . 1983 . 2479	. 3471 . 3967 . 4463 . 4959 . 5950	. 6942 . 7934 . 8926 . 9917 1. 0909	1, 1901 1, 2803 1, 3884 1, 4876 1, 7355	2. 9835 2. 2314 3. 7493 4. 9587	7, 4380
10.0	. 004950 . 009900 . 01485 . 01980	. 03960 . 04950 . 07425 . 09900 . 1238	1485 1732 1980 2475	. 3465 . 3960 . 4455 . 4950 . 5940	. 6930 . 7920 . 8910 . 9500 1. 0890	1. 1880 1. 2870 1. 3860 1. 4850 1. 7325	1. 9800 2. 2275 2. 4750 3. 7125 4. 9500	7.4250
9.0	. 004938 . 009877 . 01481 . 01975	. 03951 . 04938 . 07407 . 09877 . 1235	. 1481 . 1728 . 1975 . 2469	. 3457 . 3951 . 4444 . 4938	. 6914 . 7901 . 8889 . 9877 1. 0864	1. 1852 1. 2840 1. 3827 1. 4815 1. 7284	1. 9753 2. 2222 2. 4691 3. 7037 4. 9383	7.4074
8.0	. 004922 .009844 .01477 .01969	.03938 .04922 .07383 .09844	. 1477 . 1969 . 2461 . 2953		. 6891 . 7875 . 8859 . 9844 1. 0828	1. 1812 1. 2797 1. 378 1. 4766 1. 7227	1.9688 2.2148 2.4609 3.6914 4.9219	7.3828
N G	0.000 0.000 0.000 0.000 0.000 0.000	2020	00000 00000			ಪ್ರಪ್ರಪ್ರಪ್ರ ಕಾಹಿಡಿದ್ದರು	0.44.5 0.7.5 0.05	15.0 20.0

REDUCED FREQUENCY (k); MACH NUMBER (M)
AND FREQUENCY PARAMETER (\(\Omega\) INDEPENDENT (Concluded)

Table 1208.1

$c_{\mathbf{L}\alpha}^{*}$	13645.534 6822.3069 4547.6937 3410.2338 2272.4677	1703.2787 1361.5210 905.13392 676.18448	245.74683 379.88178 329.07816 257.96834 69018	174.51211 147.57487 126.18393 108.72628 81.858475	62.157454 47.218434 35.692177 26.745091	14.497121 10.472482 7.4852195 5.3201039	1.3358581 .94062682 .60910356	
\tilde{c}_{Llpha}	- 3689639 - 922354.28 - 409894.12 - 102418.07	- 157577 - 8 - 16887 - 808 - 16324 - 934 - 9150 - 6754 - 1692	1 2 2 3 3 5 4 4 6 7 1 1 2 2 3 3 5 7 1 1 1 0 5 6 3 5 7 1 1 1 0 5 4 4 6 7 1 1 0 5 4 4 6 7 1 1 0 5 4 4 6 7 1 1 0 5 4 4 6 7 1 1 0 5 4 4 6 7 1 1 0 5 4 4 6 7 1 1 0 5 4 4 6 7 1 1 0 5 4 4 6 7 1 1 0 5 4 4 6 7 1 1 1 0 5 4 4 6 7 1 1 1 0 5 4 4 6 7 1 1 1 0 5 4 4 6 7 1 1 1 0 5 4 4 6 7 1 1 1 0 5 4 4 6 7 1 1 1 0 5 4 4 6 7 1 1 1 0 5 4 4 6 7 1 1 1 0 5 4 6 7 1 1 1 1 0 5 4 6 7 1 1 1 1 0 5 4 6 7 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-683.96024 -508.92920 -389.53998 -304.74015	-132.11998 -92.486217 -66.841928 -49.803563	-30.364694 -24.863161 -20.970915 -18.148862 -13.654828	-10.755628 -8.4652057 -6.6211552 -2.8987917	- 1.605197 7314905 4195301
c_{Lh}^{*}	-3201.7511 -1600.7763 -1067.0740 -800.18976 -533.23948	1399 13199 13199 1318 1318 1318 1319 1319	-104.76660 -89.203081 -77.455800 -60.838321 -69.582397	1 2 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	-115. 441986 -112. 482002 -10. 033138 -8. 1912825 -6. 815253	-5.06996530 -4.53418519 -4.1552012 -5.4552012	1 2 3 3 3 3 4 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5	- 1,125767 - ,7881309 - ,6165438
\bar{c}_{Lh}	-113.220384 -113.229386 -113.226386 -113.226393	11111111111111111111111111111111111111	11111 2000 11111 1120 1120 1120 1120 11	-111.686806 -111.688148 -111.8363148 -10.812550		-4.1784821 -2.4676029 -2.3775735 -1.5873627	-1.2441897 -1.10441897 98667714 32115086	1237239 0107663 .0303910
a	00000 0000 00000 10000	00000 00000 00000 000000	00000 00000 www.a.n.n	00000	00000 111188 40808	00000 00000 40000 00000	0000 4400 0000 0000	200 200 200 200 200 200

Table 1208.2 AERODYNAMIC FLUTTER COEFFICIENTS, Lift, M = 1.1

CMa	10837.563 5418.2863 3611.6306 2708.1387 1804.3132	11035 1001 1001 1000 1000 1000 1000 1000	251.34478 2557.882613 200.522013 161.385113	132.69655 110.60116 92.963917 78.508041 56.173731	39.794888 87.466888 18.112588 11.053999	2.5.0 2.5.0 2.0 2.0 2.0 2.0 2.0 2.0 2.0 2	11.9295279 11.5435642 11.8655949	9212357 5294715 3839792
Č _K α	-1844783.7 -461141.23.7 -204911.15 -115230.63	-28753.037 -18375.762 -8126.7113 -4539.7030	- 1978 .0071 - 11434 .5624 - 1082 .0406 - 668 .01234 - 443 .80998	-309.33476 -222.76547 -164.11401 -122.84417 -70.881517	-41.702516 -24.695739 -14.710288 -8.9679793 -5.8444607	- 4 . 3310 327 - 3 . 74520 52 - 3 . 74596 40 - 3 . 95876 52 - 5 311 24	-4.4061296 -3.6769270 -2.7964271 -1.4563338	8346054 4037820 2348771
C _M h	-1600.88485 -1533.43778 -299.96261 -266.42141	-1999.58489 -159.43037 -105.73845 -78.339676	- 51 - 43. 406958 - 37. 442446 - 28. 838257 - 931509	115.583550 115.5847901 112.358900 1.0.358909			 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9	4687929 3918677 3276093
^C Mh	-111.02249 -111.02249 -111.022908 -111.020859	-11.006823 -10.996305 -10.959846 -10.908967	-10.764640 -10.671649 -10.565151 -10.313020	-9. 6640557 -8.8496948 -7.40496963	-6.22434 -4.2261331 -3.22601331 -3.22601331 -3.226001331	-1.6613287 -1.0369064 54784694 18996070	.17881652 .01088480 .07555973	.1841614 .1152396 .0946744
a	00000 00000 00000 4644	00000 00000 00000 00000	00000 00000 00000 00000	00000	00000 111100 40000	00000 00000 40000 00000	0000 448¢ 0000 0000	10 15.00 20.00 00

AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Moment, M = 1.1 Table 1208.2

$c_{\mathrm{L}\alpha}^{*}$	2227.1765 11113.5045 742.24323 556.58470	277.95750 222.16525 147.64621 110.24892	72.580172 61.703627 53.481352 41.819354 33.885040	28.090274 23.642160 20.101111 17.204053 12.730197	9.4462106 6.9406980 4.9942693 3.4913816 2.3306158	1.4452234 .78309112 .30141271 .03613290	51342939 47679891 44601913	3256125
\bar{c}_{Llpha}		11883 18810 18610 18641 19048 19048 1908 1908 1908 1908 1908 1908 1908 190	- 900 . 35570 - 657 . 99650 - 500 . 72632 - 315 . 86026	-155.17534 -1116.10226 -89.424296 -70.449967 -6:020363	-31.637984 -22.620336 -16.720089 -12.741310	-8.0756663 -6.7040440 -5.7076406 -4.9668330	-2.9792883 -2.3842118 -1.9076430 -86346896	- 4851438 - 2186748 - 1172607
$c_{\rm Lh}^*$	-1256.3656 -628.15011 -418.73039 -314.00963	11256.87408 183.472000 183.4720000 162.4720111 162.4720111	144. 135. 135. 135. 135. 135. 135. 135. 135	-16.513319 -12.187764 -12.641413 -8.2869016	-6.5875505 -5.3805783 -4.3602800 -3.6283906 -3.0717807	-2. 6515960 -2. 3376574 -2. 1055951 -1. 9352429	-1.5224688 -1.3818788 -1.2333557 -81740877	
\bar{c}_{Lh}	-4.36833711 -4.3683711 -4.3681151 -4.3616885 -4.3610914	44444444444444444444444444444444444444		-3.9622298 -3.7193840 -3.5817679 -3.5817679	-2.9558142 -2.6182053 -1.9510969 -1.6510969	-1.3584932 -1.1034445 71141724 -1.41141724	- 27450741 - 22737632 - 20282627 - 00835777	.0208292.0246040
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AERODYNAMIC FLUTTER CUEFFICIENTS (Continued), Lift, M = 1.2 Table 1208.2

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AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Moment, M = 1.2

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AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Lift, M Table 1208.2

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\bar{c}_{Llpha}	- 216670 . 15 - 54165 . 634 - 13539 . 505 - 6016 . 1489	1 + 1 2 3 3 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	- 238 . 24012 - 174 . 34934 - 1132 . 93679 - 64 . 215541	1121. 84.50008 1121. 84.40008 112.4475525 85.00008	1.69.10086568 1.50050893583 1.500508983 1.500508983 1.5585572	-2.5914939 -2.1780661 -1.68590307 -1.6331545	. 98372365 . 99573601 . 64644851 . 28990222	15844431 06673173 03612292
c _{Lh}	-530.62022 -176.85536 -1132.62956 -88.3958	1111 1556 1557 1557 1557 1557 1557 1557	117.486615 -114.927204 -112.999891 -10.283736 -8.4541837	-7.1226029 -6.12298409 -5.3409378 -4.7030100	- 23. 0336305 - 25. 50900994 - 27958026 - 17. 7958026	-11.21988442 -11.1078188 -11.0220053 -8454366	80530977 74416291 68424207 47019468	37052712 25381483 18632963
\bar{c}_{Lh}	- 11 . 353 55 35 11 . 353 55 35 35 35 35 35 35 35 35 35 35 35	11.3520131 -11.3520131 -11.3479265 -11.3434973	11.33309094 11.313454 11.313454 11.3912978 11.2912978	1.2337556 11.1989061 -1.1604808 -1.1186473	92643684 821042684 71392016 60824853		01581722 .00085726 .00078103	.001394996 .00094680 00356114
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AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Moment, M Table 1208.2

$c_{\mathrm{L}\alpha}^{*}$	122.98649 61.498649 40.979303 30.723851 20.462331	15. 325509 12. 325509 6. 1085832 6. 0285937 4. 7685907	2. 90.90 2. 90.90 2. 90.90 2. 90.90 3. 90.90 4. 90.90 4. 90.90 5. 90.90 6. 90.90 7. 90.90 8.	1.3501818 1.0786347 .85825215 .67461219		1.36964997 1.4288240198 1.437653882 1.437653882	1.37929624 1.33015930 1.288872736 1.568872736	14300283 09984772 07669007
\bar{c}_{Llpha}	-147589 59 -16896 582 -16397 521 -9822 9548	- 2304.6239 - 1474.4247 - 654.47677 - 367.49759	-1162.51984 -119.01865 -90.787898 -57.597344 -39.57944	-28.727074 -21.695293 -116.886095 -113.457688	1 1 1 6 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-1.8745775 -1.5804986 -1.3587547 -1.1881620 -89917765	71458699 57887676 47156736 20835941	11244837 04706389 02718624
c_{Lh}^{*}	-409.97067 -204.97850 -136.64474 -102.47559 -68.301883	- 151 - 240 - 251 - 263 - 263	-11.556298 -11.0.070380 -7.9779797 -6.5703191	-5.5548126 -4.7852757 -4.1805782 -3.6921047	- 2. 4153011 - 2. 0135985 - 1. 7049054 - 1. 4644828	-1.1282399 -1.0124927 -92218885 -85195830 -73681910	66988211 62049391 57413687 39617482	31120791 20600366 15147290
\bar{c}_{Lh}	91103918 91098857 91090822 91078615	900997681 900937080 900726648 900432800	89597540 89058027 88438829 86967156	83140541 78253664 75464762 6931530	62577891 55469137 41003796 340493	21527633 16197353 11585627	.00823318 .02032876 .01809028 .02317949	.00673163 00244295 00106506
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1.5 AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Moment, M = Table 1208.2

$c_{\Gamma lpha}^{*}$	47.179697 23.583963 15.716104 11.780213	5.8665816 4.6791607 3.0868374 2.2809851 1.7897934	1.2123507 1.0248416 75176107 55831534	.29307106 .19538156 .112843554 -021843554	1.12580180 1.20732396 1.31915615 1.3545586	378117198 39211777 39766716 39623596	1.28950161 1.88953161 1.855001565 1.6951565	12290792 08675039 06566161
\bar{c}_{Llpha}	-109808.19 -27451.325 -12200.054 -6862.1089	-1714.8054 -1097.1294 -487.08010 -273.56453 -174.73914	-121.05814 -88.692180 -67.687472 -42.991594	-21.507165 -16.272617 -12.691393 -10.137216 -6.8299691	-4.8602011 -3.6043618 -2.7637713 -2.1804359 -1.7641597	-1.2330398 -1.2330398 -1.0620571 92905178		08593307 03639067 02192133
c_{Lh}^{*}	-334.57150 -1167.28085 -111.51512 -83.630624 -55.742865	-41. 795725 -33. 4295725 -22. 256093 -16. 6654673	-11. -9.4664220 -8.2359098 -6.53284710	4.00 4.00 6.00	- 1. 69494957 - 1. 6943441 - 1. 248827 - 1. 0936161	97152735 87501613 79886801 73890171 63857184	57940231 53690947 49851814 34417128	26844212 17381573 12921516
$ ilde{c}_{\mathrm{Lh}}$	653445 653445 653455 653456 654275 654275 654275	65270160 65227174 65078095 64869842 64602871	64277765 63895235 63456113 62412033 61154567	55 80 6 9 4 5 8 9 6 9 9 8 9 9 9 9 9 9 9 9 9 9 9 9 9 9	450117391 39909581 34670702 29448735	19588241 15171638 11208600 07751766	.02697331 .02397678 .02397678	.00218567 00298764 .00067444
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AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Lift, M Table 1208.2

C**	- 1.6 . 2.9 . 4.6 . 9.9	-2.0885467 -11.6857624 -1.1583353 90486219	67156486 61338190 57456224 53140908	511181693 52764806 52057144 54057144	59647983 618862993 63451018 642553111	621660927 621660927 60180929 57719711	42398680 35474175 30188816	14441633 10288064 07716180
C _M α	-54903.668 -13725.235 -6099.5997 -3430.6273	-855.97595 -843.118823 -136.35823 -86.947344	-60.109046 -43.928660 -33.429282 -21.088420	-10.364629 -7.7585442 -5.9803173 -4.7167073	-2. 1407265 -1. 5474879 -1. 1627730 -90657444	61342303 53017800 47105568 42782669	- 30 3638 47 - 254119 56 - 20665389	04014228 01635466 01158598
C,*	-167.28412 -83.637157 -55.752660 -41.808779	-20.884805 -116.696106 -111.103621 -8.2993503	-5. 4793294 -4. 6670316 -4. 0540960 -3. 1874422	-2.1748056 -11.8499808 -11.5932795 -1.3849395	688834110 54087806 54087803 44559866	235548199 239138261 256981799 25786010	1. 26439095 1. 26424105 1. 26424105 1. 18457393	14625155 08641163 06366423
Смһ		54371411 54324133 54160186 53931217	552880577 552880577 5523788486 51233612	4 6 8 2 6 1 4 7 0 4 6 4 6 6 3 3 7 5 4 2 3 4 2 6 4 8 5 3 5 8 8 8 8 7 6		06421889 01356901 .01356901 .04316302	.09961770 .08706459 .06523880 .02650529	.00001465 00462843 .00139123
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AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Moment, M = 1.6 Table 1208.2

$c_{ m L}^*$	8.2395430 4.1157011 2.0497108 1.357432	1.0085844 .79711197 .50885712 .35802576	.19396083 .14151254 .09899721 .03205630	1.064454 1.1064413460 1.1361842860 1.16655620	1.286221697 1.324594197697 1.324599538 1.344892248	 	1.25293879 1.25293879 1.14638178	10863911 07673344 05737442
\bar{c}_{Llpha}	-86617.957 -9623.6241 -5412.9966	-1352.7489 -865.51950 -384.30601 -215.88243	-95.583125 -53.482881 -34.001371	112.051260 112.9201260 110.093494 5.0765653	-3.9039523 -2.9074602 -2.2389708 -1.7731119	-1.1941457 -1.0106562 87061651 76168951 57494726	1. 36912633 1. 36912633 1. 20136649	06920391 02992692 01816890
$c_{\rm Lh}^*$	-283.23146 -141.61206 -94.403954 -70.798679	11111111111111111111111111111111111111		1.3. 883 1.2. 9843 1.2. 9445 1.2. 61176 1.0. 1763 1.0. 1	11111 11	85917431 77610987 65732025 56732025	1. 51393244 1. 47590596 1. 44261440 30516800	23598458 15123326 11374445
$ ilde{c}_{\mathrm{Lh}}$	49001520 489998858 489984421 489988211	 4488944884848848886944884886949894889898989	48208843 47924751 47598573 46822786	44 48 0 19 10 44 35 7 35 7 25 40 73 13 11 40 73 13 11			.02090676 .02835650 .02518664 .01158654	00036854 00240861 .00120876
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AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Lift, M Table 1208.2

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. 1	405-00	44050	4WW.00	निचन्त		• • • • •		
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AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Moment, M = 1.7 Table 1208.2

$c_{\mathbf{L}\alpha}^*$	11.3.10.05.46 13.30.05.446 13.30.05.746 12.30.05.746	.1.6637673 -1.3381046 90846104 69851284 57640785	49818723 44500457 40743079 36022872 3451628			34793878 34647781 38647781 38711111	26088904 22676876 19800778	09789305 06874835 05102601
$\overline{c}_{\mathbf{L} lpha}$	-71192.971 -17797.878 -7909.8982 -4449.1052	-1111.9121 -711.4917 -315.93075 -177.50013	-78.623464 -57.638758 -44.019890 -28.006911 -19.312189	-14.073311 -10.676866 -8.3520464 -6.6928383 -4.5414665	-3.2565172 -2.4339584 -1.8803851 -1.4935949	-1.0102882 -85607458 -73786196 -64554408 -48656338	38491463 31165775 25452654 10779498	05792872 02562395 01528985
c_{Lh}^*	-246.09894 -123.09894 -82.027917 -61.517616	- 24. - 16. - 16. - 174. - 175. - 175	-8.1469174 -6.9658206 -6.0778013 -4.8294765		-1.5405839 -1.3047285 -1.1224718 97911378	77395549 70083797 64215442 59504339	1	21052197 13471101 10213041
\bar{c}_{Lh}	37977843 37975798 37972389 37967617				26 28 15 0 1 23 3 3 0 4 9 8 0 17 1 4 8 4 4 8	11250745 08569747 06137013 03988800	.02138163 .02749823 .02440888	00164645 00155118 00100945
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1.804883 -1.381 3.801880 -1.141 45872099869 84416508814 1514638061	7224517085 1132806502 851406 - 6121	222720 669858 498912 - 5827	903754 5039 727059 4632 198607 4613 791584 4385 038359 3793	005520 3220 484680 3723 224227 2723 348317 15375	213461151 293970811 104250596
3.804883 4.801880 1.1.144 8441650 1.986 151464 151467 1.881	722451 - 708 113280 - 650	22272720 669858 198912 198912 198912 198912 198913	903754 - 503 198607 - 483 791584 - 461 038359 - 379	005520 www. 224227 www. 348317 hww.	21346115 29397081 10425059
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AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Moment, M Table 1208.2

$c_{\mathbf{L}\alpha}^{*}$	-25.478348 -12.4741407 -6.3751684 -2550721	1.3.56650 1.1.3.05650 1.3.037441 1.3035153 1.3035153 1.3035153 1.3035153		46 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4			23659960 20579851 117986018	08942962 06224005 04607191
$c^{\Gamma lpha}$	-60308.788 -15076.922 -6700.6500 -3768.9550	-941.96353 -862.78470 -867.67443 -150.40745	-66.647091 -48.870404 -37.333411 -23.768017 -16.401929	-11.963240 -9.0852079 -7.1148756 -5.7083099	1.2.7.9.3.5.1.1.6.2.1.4.3.1.1.0.0.3.1.1.4.3.1.4.3.3.5.3.5.0.0.5.1.4.3.3.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5	87627629 74319906 64081680 56059430 42191814		04992360 02252339 01305355
$c_{ m Lh}^*$	-218.01358 -109.00453 -72.667168 -54.497734 -36.326793	-27.239816 -14.511744 -10.870680 -6830953	- 7 . 22 22 28 4 28 - 1 . 2 . 3 9 0 9 5 0 3 . 3 9 6 6 8 8 6 . 5 . 5 . 5 6 6 8 8 6 6 8 8 6 8 6 8 8 8 6 8 8 8 6 8 8 8 6 8	-3.01139064 -2.01139064 -2.01139064 -2.0436512 -1.6601312	-1.3838626 -1.1761500 -1.0154670 88881234 7878379	70662371 64117614 58830110 54553304	39157498 36429988 36489988	19006287 12210497 09289662
\vec{c}_{Lh}		30161571 301462520 30075101 29981321				089028994 06735173 04759733 03007128	.02060134 .02571929 .02281766	00216224 00076647 00054994
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AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Lift, Table 1208.2

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C,*	-98.012801 -49.004563 -24.498607 -16.328323	1123.241959 19.7891650 16.5159384 14.8763107	- 2 . 2307591 - 2 . 4022417 - 1 . 9007679	-1.3191725 -1.1341757 98868217 87107975 69251473	56378995 39426774 33797472 34797472	25196492 211960549 201060545 20106592	18623003 18163003 18163009	09017883 05521498 04316605
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2.0 AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Moment, Table 1208.2

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AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Lift, M Table 1208.2

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C.M.C	-60.000415 -30.001378 -20.008219 -15.003029	-7.5061914 -6.0071572 -4.0116528 -3.0155264	-2.0231984 -1.7412739 -1.5307407 -1.2381148	90934878 80885092 73185117 67117661	51980505 473659965 43757454 407966112		1.22247045 1.19079399 1.16549184 1.11032335	08453943 05677331 04229570
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c# wh	-81.894391 -27.295874 -20.470426	-10.230141 -8.1810729 -5.4470241 -4.079172	-2.7047159 -2.3106580 -2.0141433 -1.5967769	1.960138935 1.960138935 1.94046835 1.94340854		23855948 21698217 20072993 18874095	1.16536295 1.16186595 1.15696458 1.10378179	07531876 04849869 03705195
c _{Mh}	14100093 14099115 14097115 14095200	1.14079550 1.14067819 1.14087131 1.13970286 1.3897402	1.13808629 1.13704150 1.13584180 1.13298790	12555024 12102715 11601533 11055504	08513947 05642111 05486946 08172811	01436246 00209154 .00882202 .01817928	. 03938801 . 03609659 . 02753303	00324324 .00086297 00085760
a	00000 00000 46440	00000 00000 00000 00000	00000 00000 00000 00000	00000	00000 111100 40000	00000 00000 40000 00000	0000 4400 0000	20.00 20.00 00.00

$c_{\mathbf{L}\alpha}^*$	-40.947725 -13.650617 -10.238866 -6.8276299	-5.1225270 -4.0998767 -2.7375401 -2.0576477	-1.3802768 -1.1878057 -1.0440601 84423798 71254269	551070455 551079085 49852237 45714204 39647230		 	1.14634345 1.114634345 1.1255345 44055445 44055445 4405445 4405445	06381017 04254889 03197136
$ar{c}_{\mathbf{L}oldsymbol{lpha}}$	-34181.890 -3545.3765 -3797.8741 -2136.2482 -949.37262	- 533 . 96620 - 341. 69241 - 151. 79251 - 85. 327761	-37.853536 -21.238390 -13.548853	- 5. 85 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	-1. 6444504 -1. 2444504 - 97091475 - 77861364 - 63850 284		20055656 16144672 13170016	03046248 01418174 00754892
$c_{\rm Lh}^*$	-141.23759 -70.617873 -47.077561 -35.307098 -23.536023	-17.649874 -14.117695 -9.4067042 -7.0496958 -5.6342926	-4.6897048 -3.5068014 -2.7948273 -2.3184172	-1.9767169 -1.5182080 -1.3566130	93759816 80587130 70367236 62260625	50 0 4 0 4 1 1 9 0 4 0 1 1 9 0 1 1 2 0 0 1 1 2 0 1	30331683 27751055 25684121 17423752	12893701 08581543 06438860
$ar{c}_{\mathtt{Lh}}$	1 1222 1222 1222 1222 1222 1222 1222		120069418 11922419 117322419	11246076 10947568 10615858 09445884	08547520 07582421 06575795 05553042	03556383 02626330 01767307 00993371	.01346082 .01594488 .01412114	00128644 .00067990 00043523
a	00000 00000 00000 40040	00000	00000 00000 00000 00000	00000	00000 44000 40000	00000 00000 40000	0000 0000 0000 0000	200 200 000 000 000

AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Lift, M

C. Mα	-57.662911 -28.832261 -19.222402 -14.417741	-7.2120898 -3.7716020 -3.8521961 -2.8938190	11.9380576 11.6660836 11.4627303 19.1794977		. 4 7 8 8 4 7 4 1 . 4 2 8 8 5 3 9 6 0 . 3 9 2 4 0 1 7 8 . 3 6 3 0 0 1 7 8		1.19407216 1.16725884 1.14574223 1.09748092	07506921 04962161 03735068
$\tilde{\mathbb{C}}_{M\alpha}$	-17090.891 -4272.6345 -1898.8833 -1068.0704 -474.63260	- 266.92942 - 170.79256 - 75.842737 - 42.610535	-18.873919 -13.836334 -10.567037 -6.7231480 -4.6361647	-3.3788575 -2.5639017 -2.0062510 -1.6084329	78584706 58971303 45820813 36675723 30133160	25342148 21760496 19028750 1690983 13211508	- 10746927 - 08817602 - 07163603	- 01455025 - 00743542 - 00353965
c _{Mh}	-70.618486 -35.308324 -23.537861 -17.652323	-8.8224867 -7.0557865 -4.6987675 -3.5187485 -2.8095436	-2.3357607 -1.9965203 -1.7413849 -1.3825637 -1.1415849	96819245 93704681 73421715 65132427 52582930	367850282 36784265 31589498 27545181	21898419 19967874 18479061 17345505	14813595 14335196 13815262 09065714	06481550 04337622 03236456
^C Mh	10216649 10215945 10214773 10213132		1.0000 7076 1.009931932 1.009845634 09640886	09104739 08417341 08023350 07149586	06184277 05156364 04095730 03032266	01009688 00100695 .00712520 .01415123	.02814223 .02814223 .02150152	00202888 00101579 00067786
a	00000 00000 00 10000	00000	00000 00000 00000 00000	00000	00000 111100 40000	00000 00000 40000		20.00

AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Moment, Table 1208.2

_								
$c_{\mathbf{L}\alpha}^{*}$	-40.643626 -13.548873 -10.162307 -6.7761166	1.5. C6833941 1.2. 7151449 1.3. 03961281 1.63561281 6356228	-1.3659057 -1.1741886 -1.0308413 83118583	60579079 536579079 48315804 37875804 37875804		226573 20200503 19120803 19120803 18488	1.124593376 1.1262131 1.11262121	05749734 03800379 02870488
$\tilde{c}_{L\alpha}$	-29228.459 -7307.0451 -3247.5241 -1826.6917 -811.81151	- 255 - 125 - 125	-32.384464 -23.768711 -18.176942 -11.601539		-1.4190057 -1.0749386 84105958 67557624 55472435		- 17363582 - 13951511 - 11374170 - 04649770	02663555 01231412 00661221
c_{Lh}^{*}	-124.52355 -62.261082 -41.506621 -31.129160 -20.751239	-15.561819 -12.447800 -8.2947070 -6.2170240 -4.9695138	1.3.54189994 1.3.0949995 1.2.4679995 1.2.4679995 1.2.467995 1.2.467995 1.2.467995 1.2.467995 1.2.467995 1.2.467995 1.2.467995 1.2.467995 1.2.467995 1.2.467995 1.2.467	-1.74811111 -1.5218344 -1.3451590 -1.2032789	83577544 72030976 63067598 55947499	45496507 41620402 38402826 35717448	. 27379797 . 24971825 . 23054777 . 15589626	11476600 07706564 05749754
\ddot{c}_{Lh}	09210196 09209719 09208923 09207809	09200172 09194447 09174587 09146833	09067850 09016762 08958057 08818228	08452587 08229330 07981117 07709660			.01112201 .01307697 .01157608	00078436 .00063021 00028201
G	00000 00000 00000 148842	00000 00000 00000 011400 00000	00000 00000 0000 00000 00000	00000	00000 111166 40006	00000 00000 00000 00000	0000 4487 0000	20.00

AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Lift, M = 2.6 Table 1208.2

								
c.*α	-54. -27.3123766 -18.208956 -13.657396		18323260 136421260 13608847 1111144607	00633573 01211449 63941819 58172920	43576975 35571128 35571128 35571128		1.17263753 1.149361753 1.13066937	06760818 04427658 03354327
$\widetilde{\mathbb{C}}_{M\alpha}$	-14614.191 -3653.4839 -1623.7234 -913.30719	111228.26.26.307 1646.05782 24.867561 24.451140	-16.154180 -11.846535 -9.0509155 -5.7638461 -3.9790371	11111 2311 2411 2411 2411 2411 2411 2411		22250466 19087077 16658835 14756809	1.09242993 1.07554637 1.06134945	01300626 00643320 00317421
CMh	-62,261543 -31,130081 -20,752620 -15,563659	-7.7790688 -6.2216001 -4.1439092 -3.1039295	-2.0617183 -1.7630084 -1.5384454 -1.2228291 -1.0111263	85889030 74390897 65385147 58132650		20237272 18488414 171116080 16047362	1.13439067 1.128779067 1.12336089	05708455 03916046 02875961
⊡Mh	07675121 07674596 07673720 07672495	07664094 07657798 07635956 07605438	07518627 07462503 07398041 07244619		04654788 03881278 03081291 02277026	000740148 00045472 .00578826 .01120618	.02234181 .02234181 .01708841	00108694 .00088499 00041776
a	00000 00000 00000 1488440	00000	00000 00000 00000 00000	00000	00000 11111111111111111111111111111111	00000 00000 40000	0000 0000 0000	15.00 20.00

$c_{\Gamma lpha}^*$	-139.485203 -13.743022 -9.8723529 -5.5825036	-4.9378590 -3.9512961 -2.6365300 -1.9798410	-1.3245240 -1.1378695 99820963 80346078 67445726	514 898 403 468 448 833 480 8833 80 88 559		20767912 19515468 18392750 17369060	1.13211240 1.11584228 1.102333233 06786333	05237224 03444719 02608485
\bar{c}_{Llpha}	-25583.549 -6395.8351 -2842.5546 -1598.9065	-399.67439 -255.76656 -1113.63545 -63.889676	-28.357302 -20.815925 -15.921420 -10.165870 -7.0399070	- 5. 1555713 - 3. 9330910 - 3. 0954882 - 2. 4968766 - 1. 7185098	1. 2509220 1. 744368447 1. 59809038 1. 59809058 4 9158564	411609 32 35022467 30220 355 26398638	15337538 12303583 10024450	02374173 01086416 00592356
c_{Lh}^*	-111.60166 -55.800294 -37.199603 -27.899080	113.947406 111.156646 17.4348070 15.5730091	-3.7094783 -3.1763120 -2.7760220 -2.2146486 -1.8393728	-1.5704960 -1.3681765 -1.2102863 -1.0835537	75557588 65258371 57260054 50899598		22 49 94 83 0 20 93 94 83 0 20 93 93 93 83 83 83 83 83 83 83 83 83 83 83 83 83	10364872 06997122 05204393
\bar{c}_{Lh}	07117353 07116986 07116374 07115517	07109644 07105242 07789969 07068626	06968585 06923427 06815848 06815848	06534256 063534256 061711300 05962092		02048856 001495668 00981361 00515015	.00922724 .01079551 .00955305	00040360 .00049691 00010207
a	00000 00000 00 10000	00000	00000 00000 0000 0000 0000	00000	00000 111100 40000	00000 00000 00000 00000	0000 4480 0000 0000	200 000 000 000

2.8 AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Lift, M Table 1208.2

C,KQ	.504728 .159810 .169018 585817673	4403803 1533499 4379837 5810190 0674096	7254722 4816271 2990837 0443168	5528101 6580256 9665021 4168137 5994794	0213956 5900912 2541667 9828605 7567550	556312318 2434021 2417651 1042045 8060997	5581376 3556931 1871301 7965954	6154653 4012481 3048169
	11111 2044 4044 4044		 ਜਜਜਜ !!!!!	11111 -0004	1 1 1 1 1 4 w w c c c	11111		000
<u>C</u> Mα		80830 85441 88918 916125	150 20 20 20 20 20 20 20 20 20 20 20 20 20	514137 229557 245674 741686	588331 739053 720615 698266 626389	2720 3229 5429 5429 120 106697	115296 610589 366398 849097	179878 562587 893451
	1111 1211	11111 44240 9440 95	11111 441-82 40 · · ·	0444 ••••®	1 1 1 1 1 0 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	11111 	0000	011 005 002
c _M h	555.8000550 118.5599251 113.948828 9.298888	6.9722807 3.71147417 2.7829631 2.2329631	1. 58494593 1. 5840205 1. 3810311 1. 0986952 . 90947051	. 670951906 . 59065100 . 526065100 . 52605100	25631604 26518611 233338267 208114 208114 208174 208174	.17809933 .17809988 .15937757 .14930170	. 12312403 . 11699600 . 11144488 . 07261448	.05118396 .03559996 .02594736
^C ⊮h		05922615 05917773 05900977 05877508	05810740 05767570 05717982 05599939	05291773 05103982 04695547 04668027	03602564 03004019 01759031 01759031		. 01935740 . 01802001 . 01379317	00042228 .00066761 00013376
U	00000 00000 00000 HWW40	00000	00000 00000 00000 00000	00000	00000 111100 40000	00000 00000 40000 00000	4487 0000 0000	15.00

2.8 × AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Moment, Table 1208.2

$c_{\mathrm{L}lpha}^{\mathrm{L}lpha}$	-137 -118.9988311 -12.6613481 -9.4963910	11.2.0000000000000000000000000000000000	-1. 2725315 -1. 0927226 95812194 77028047			1.17966977 1.16895035 1.159265035 1.15926502	1.12083863 1.10610384 1.09390548	04811509 03157571 02392277
\tilde{c}_{Llpha}	- 522789 - 52597 - 52597 - 1424 - 2746 - 532 - 635 - 6	-356.02825 -101.23181 -56.919483	-25.268070 -118.550363 -114.190420 -9.0634259 -6.2787842	- 4. 600013 48 - 2. 76110 324 - 2. 23113 483 - 33113 453	- 1 1 2 0 6 3 3 0 6 6 7 7 8 9 8 1 2 6 6 7 7 8 9 8 1 8 6 4 7 8 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9	- 37045896 - 31528967 - 27205235 - 23758305	13756631 11019196 08973122 03683936	02145984 00971385 00539899
$c_{ m Lh}^*$	1101. 150. 150. 150. 16. 16. 16. 16. 16. 16.	-112.658449 -10.125748 -6.7481607 -5.0586726	-3.3678141 -2.88841350 -2.5210472 -1.6717530	-1.4280970 -1.2448299 -1.1018674 98716271	69053235 59745838 52510299 46753878	38257579 35077818 32417479 30176692 25938412	. 23019986 . 20887527 . 19198125	09468064 06409111 04762340
$\overline{c}_{\mathrm{Lh}}$		05620810 05617344 05505317 05588509	05540670 05509721 05474152 05389406	05167641 05032115 04881333 04716297	03936528 034936528 03027476 02552170	1.0161528C 1.01174099 1.00763034 1.00389422	.00898340	-,00013436 .00035068 .00003675
U	00000 00000 00000 40040	00000	00000 00000 00000 00000	00000	00000 111100 40000	00000 40000 40000	0000 4487 0000 0000	20.00

= 3.0 AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Lift, M Table 1208.2

ς*,	-48.532901 -24.256787 -16.178232 -12.134067 -8.0901259	-6.0683795 -3.2388706 -2.2388726 -2.4311081	-1.6244382 -1.39442192 -1.2221726 98163679	70838238 523644238 55807921 50590104		21852437 21861968 20450730 19179692	14221099 12379931 10894970	056511112 03678860 02795077
Č,Mα	-11394.579 -2848.6079 -1266.0206 -712.11505	-117.99188 -113.89712 -50.593725 -28.437633 -18.182635	-12.612131 -9.2534103 -7.0735913 -4.5104569 -3.1185741	-2.2797596 -1.7357872 -1.3632906 -1.0972900		15402684 15402679 13405109 11828291	- 07239529 - 05879771 - 04771721 - 01661429	01080753 00497682 00273715
C.*	-50.642511 -25.320834 -16.880087 -12.659573 -8.4387780	- 5. 3280998 - 3. 37194688 - 2. 5265363 - 0187363	-1.6797323 -1.4372161 -1.2550042 99915492	70476959 61200367 53946378 48113367		1.16094794 1.14909292 1.13958124 1.13958124	11369544 10726312 10165201	04653532 03256799 02370476
Ē _M h	04689042 04688723 04688193 04687451	046883465 046683365 046653851 04646843	04594261 04580259 04521199 04428206	04185347 04037289 03872897 03693381	02851644 01886368 01390283		.01578414 .01473772 .01128685	.00002234 .00045086 .00007811
a	00000 00000 00000 40040	00000 00000 00000 0011000	00000 00000 00000 00000	00000	00000 111100 40000 40000	00000 00000 40000 00000	4486 0000 0000	200 000 000 000

3.0 ¥ AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Moment, Table 1208.2

c_{Llpha}^{*}	1186. 1186. 118. 118. 118. 118. 118. 118	-4.5478877 -3.6389270 -2.4273774 -1.8220270	-1.2175158 -1.0451524 91608246 73585906 61621809		28049748 226202391 20716964 19149840	1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.	09797800 08685662 05770469	0451644 02919638 02210297
\bar{c}_{Llpha}	- 50577 - 5144 - 3388 - 5286 - 3338 - 1286 - 3336 - 571 - 551 85	-321.47893 -205.73118 -91.412462 -51.400980	-22.821546 -16.755821 -12.819016 -8.1895701	1.4.1593006 1.2.5018897 1.3.02008897 1.3933593	-1.0165337 77297082 60691662 48898109	23730298 28712556 24774193 21630041	1 . 12487566 1 . 09989694 1 . 08130819	01960436 00878487 00495426
$c_{ m Lh}^*$	1 1 9 2	-11.603107 -9.2816709 -6.1858973 -4.6374508	-3.0878999 -2.6447064 -2.3120465 -1.8457051	-1.3110926 -1.1433717 -1.0125813 -90767787	63656319 55150378 48541299 43277500	35492738 32569634 20116957 28044075	1.21353086 1.19334757 1.17736910	08727788 05913934 04396208
\bar{c}_{Lh}	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		04463864 04439008 04410441 04342368	 0.44164189 0.0400464189 0.0400460464 0.040046464	03173680 028173680 02440618 02056671	01298289 00940317 00606188 00301917	.00648175 .00753757 .00666654 00232075	.000022036 .00022036 .00012198
C	00000 00000 40040	00000 00000 01100 00000	00000 00000 0000 00000	00000	00000 1111488 40000	00000 00000 00000 00000	0000 4.00 0000 0000	200000000000000000000000000000000000000

3.2AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Lift, M Table 1208.2

c_{Mlpha}^*	-45.783510 -15.861643 -11.446543	-5.7243348 -4.5801054 -3.0546776 -2.2927018	-1.5313910 -1.3142379 -1.1515809 92434586	66594893 58571759 52358680 47409941 40031317		21636221 20141782 18822672 17641167	13095405 11426290 10079621	0522588 03403103 02581871
\bar{c}_{Mlpha}	-10288.652 -2572.1337 -1143.1489 -643.00426	-160.72192 -102.84806 -45.688740 -25.683056	-11.393501 -8.35607424 -6.3924603 -4.0780228 -2.8211422	-2.0636352 -1.5723394 -1.2358630 -99553394 -68341518	49639099 37607893 23459588 23719745	1.16441971 1.146441971 1.12236827 1.10781657 1.00781655	1 0 0 5 2 9 8 0 0 8 1 0 1 5 1 5 6 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	
C _M h	-46.419451 -23.209385 -15.472546 -11.604013	-5.8006476 -3.6397035 -2.3164696 -1.8511533	-1.5405864 -1.3184443 -1.1515760 91735319	64806700 56329241 49704200 44379980 36348154	30582069 26257185 20281282 18177402	16483537 15113796 14004056 13104489	10567335 09908216 09346769 06081009	04277200 02997552 02187262
$\overline{c}_{\mathbf{M}\mathbf{h}}$	03777558 03777303 03776877 03776281	03772196 03769135 03758514 03743672	036741445 03674137 03642765 03568066	03372926 03253917 03121740 02977355	02299639 01917673 01520829 01119774	00346277 .00007250 .00327743 .00608691	.01303728 .01220223 .00934878	.00030733
บ	00000 00000 0 00000 48840	00000	00000 00000 00000 00000	00000	00000 HHHMM 	00000 00000 00000 00000	0000 440 0000 0000 0000	200 000 000 000

H 3.2 AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Moment, M Table 1208.2

c _L a	-34.768315 -117.384365 -11.589807 -8.6925975		-1.1630608 99817324 87467099 70215063	50602006 44514434 39802535 36051031	26504801 23554378 21264857 19428467	1.15632703 1.115632703 1.14554319 1.13685946 1.13685946	1.10349471 1.09108149 1.08085935	04143149 02718295 02054848
\tilde{c}_{Llpha}	-18781.280 -4695.2942 -2086.7783 -1173.7977	-293.42353 -187.42353 -83.438170 -46.919022 -30.015934	-20.834074 -115.2997768 -11.704561 -7.4791385	-3.8005135 -2.9027727 -2.2875424 -1.8477274	- 93132478 - 008132478 - 55691430 - 44898475	3099713C 26389845 22769177 19875252	1.11445322 1.09145472 1.07440456 1.03078469	01806031 00802261 00457290
$c_{ m rh}^{*}$	-85.782981 -28.891812 -21.445050 -44.2050	-10.721412 -8.5764631 -5.7161005 -4.2854611	-2.8539176 -2.4445248 -2.1372632 -1.7065913	-1.2130418 -1.0582708 -93761337 -84086465	59095752 51258088 45167231 40313485		1.19924274 1.18008423 1.16491954 11069350	08104943 05491578 04087199
$ ilde{c}_{\mathrm{Lh}}$	03710281 03710281 03709776 03709334	03706303 03706303 03696148 03685130	03653468 036434468 03610153 03554513	03409059 03320069 0321037 03112572	02599218 02306326 01998730 01683770	01060583 00765845 00490335 00239046	.00549340 .00634580 .005634790	.00016601 .00011461 .00016245
a	00000 00000 0 00000 10040	00000 00000 044000	00000 00000 00000 00000	00000	00000 111100 10000 10000	00000	000 000 000 000 000 000	200 200 000 000 000

× AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Lift, Table 1208.2

C.W.C.	-43.270818 -21.635623 -14.423987 -10.818240	-5.4099768 -4.3284951 -2.8868507 -2.1663815	-1. 2412534 -1. 2412534 -1. 0874040 87240573 72948971	552174183 552170209 49277922 44581652		 1000964 1 117450248 11634688238 103460248 10346232 10346232	12146318 10618894 09386468	04860992 03169960 02399713
ČΜα	-93390.6259 -12347.62330 -11043.3750 -286.88474	- 1146.69771 - 93.875278 - 41.705019 - 23.445491	-10.403146 -7.6350772 -5.8385700 -3.7260885	-1.8873765 -1.4388728 -1.1316653 91220372 62708433	45610403 34601076 27133526 21863674 18026558	15160392 12971812 11267465 09915381	059669940 04824243 03913357 - 01398652	00924826 00402773 00237921
CMh	-42.891398 -21.445421 -14.296638 -10.722154	-5.3599647 -8.8873051 -2.8566626 -2.1408841 -1.7110553	-1. 4242056 -1. 2190626 -1. 0649910 84879344 70413748	60039641 52226139 46123115 41220787 33829723	28526157 2854000 231471260 119041800	1.15523097 1.15223097 1.15261338 1.12348810	09875484 09210477 08652892	03965428 02774954 02034128
€Mh	03091884 03091876 03091328 03090842		1.03029752 1.023027458 1.02981845 1.02920852 1.02947858	02761479 02564254 02556245 02438228	01883799 01240935 01245556 00916344	00280107 .00011396 .00276166 .00508777	.01089141 .01021378 .00782769	.00048141 .00012173 .00026110
ប	00000 00000 0 00000 48848	00000 00000 011400 00000	00000 00000 0000 00000	00000	00000 111100 40000	00000 00000 00000 00000	0 0 4 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	20.00 20.00 20.00

AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Moment, M = 3.4 Table 1208.2

		· · · · · · · · · · · · · · · · · · ·						
$c_{\mathbf{L}\boldsymbol{\alpha}}^{*}$	-33.223700 -116.612020 -111.074869 -5.53794499	-4.153854 -2.353854 -2.5166029 -1.6634392 -1.33176536	-1.1108301 95317589 83506916 67003355	48227063 378393774 37875117 34275189		1.15605076 1.14567537 1.13620887 1.12796739	09666019 08514555 07568508	03875601 02545018 01920483
$\vec{c}_{\mathbf{L}oldsymbol{lpha}}$	-17292.248 -1921.348 -1080.7390 -480.31279	-270.16361 -172.89457 -76.826412 -43.202602 -27.639631	-19.185724 -14.088339 -10.779996 -6.8895392 -4.7764083	-3.5024658 -2.6758390 -2.1093173 -1.7042970	86019273 65506451 51504702 41545289	28701787 24438496 21084694 18401416	10573200 08440095 06863935	01675215 00738794 00424077
$c_{ m rh}^*$	- 799 - 789 982 4 - 196 - 596 198 1 - 196 - 596 198 1 - 136 - 994 681 7 9 9 9 4 68 7 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9	-9.9725166 -7.9774600 -5.3170277 -3.9864314 -3.1877724	-2.6550850 -2.2743845 -1.9886791 -1.5888718	-1.1295396 -1.98573963 -1.87366234 -1.78381497 -1.64866777	55183947 47911038 42258327 37751684 34088651	31066516 285416399 26417406 24611064	18683939 16860815 15417524 10337674	07572487 05127364 03822197
\bar{c}_{Lh}	03078265 03078108 03077846 03077846	03074971 03073090 03066565 03087445	03031483 03014684 02995375 02949357	02828856 02755155 02673103 02583227 02382324	02157576 01914503 01659037 01397238	00878488 00632739 00192680 00192680	.00468971 .00543476 .00480497 00197071	.000023942
a	00000 00000 10000	00000 00000 04400 00000	00000 00000 00000 00000	00000	00000 1111100 40000	00000 00000 00000 00000	000 000 000 000 000 000 000	10.00 20.00 20.00

AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Lift, M Table 1208.2

_			 					
C,*	8 924 6126 1466 1466 1466 1466 1466 1466 14	40446 00088 40088 60140 70144	00048 00048 00048 04000 00000 00000	24 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000	727 419 419 419 419 41 68 99 89	33835 25121 88614 01917	44985 69287 42294
	1111 400 1100 100 100 100 100 100 100 10	11111 24661 10000 10000	11111 1111. 1111. 1111. 1111. 1111. 1111. 1111.	11111 	11111 	11111 44000	1111	111 000 400 800
C _M α	.1124 .5089 35798 14486	07027 35758 01706 89338 08401	15052 28812 87884 37476 74088	07016 76879 47603 61466	28181 69338 9445 94558 38017	75 75 75 75 75 75 75 75 75 75 75 75 75 7	934486 931069 93809	619 52 678 44 21 3 66
	1 8 6 4 6 1 1 2 4 6 6 1 1 2 5 4 6 0	11111 18201 2001 2001 1001	0 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 -	11111 141 	11111 4 W M M H M M N D D M O H M L	11111 44400 46000	1111 0000 4484 448W	- 00 B
C**	-39.894835 -19.947187 -13.297868 -9.9731317 -6.6482417	-4.9856431 -2.9879613 -2.6573625 -1.9916838	-1.3252581 -1.1345373 99131875 79039988		286743037 23056732 20204073 17948123	14668157 13468684 12484795 11675132 10212074	09272011 08608001 08057285	03702074 02582826 01903575
\vec{c}_{Mh}	02565207 02565034 02564747 02564344		02513773 02474111 02423611 023623611	02291626 02211090 02121602 02023800	011564003 01033926 01033926 00760127	00230076 .00013878 .00234656 .00429506	.00919100 .00863313 .00661787	.00058029 .00001319 .00027075
ប	00000 00000 10000	00000 00000 00000 000000	00000 0000 0000 0000 0000	00000	00000 111144 40004	00000 40000 00000	0000 4487 0000 0000	10.00

$c_{L\alpha}^{*}$	-31.761898 -15.881090 -10.587551 -7.9408276	-3.9709784 -3.1771218 -2.1188635 -1.5899676	1. 06115324 1. 91074543 1. 79776650 1. 63985678	1111 44.000 44 44.000 44.000 44.000 44.000 44.000 44.000 44.000 44.000	23825721 21095268 18975385 17276419	11.11.11.11.11.11.11.11.11.11.11.11.11.	1.09071767 1.07997584 1.07116856	03641268 02393860 01803175
\bar{c}_{Llpha}	-16036+356 -1781-7965 -1002-2503 -455-43154	-250 . 34499 -160 . 34037 -71 . 249405 -40 . 067606	-17.795000 -13.067815 -9.9997361 -6.3918040	1.2.2506412 1.9.58506412 1.9585183 1.5885183 1.094093	- 79983755 - 60944766 - 47943085 - 38689648	28744171 19647649 17144426 12100589	1	01562782 00685235 00394918
c_{Lh}^{*}	-74.629005 -37.314309 -24.875991 -18.656767	-9.3276087 -7.46285 -4.9733414 -3.7288817 -3.9819529	-2. -2. -1. -1. -1. -1. -1. -1. -1. -1	1			1.17595737 1.15857008 1.14480074	07111172 04810225 03591861
\bar{c}_{Lh}				02343 023413 0234480 021694480	01611988 01607881 01393839 01173121	00036428 000529264 00335175 00157714	.00403137 .00466620 .00412488	.00028183 00002674 00016194
q	00000 00000 00000 10000	00000 00000 011400 000000	00000 00000 00000 00000	00000	00000 111444 40804	00000	0000 0000 0000	000 000 000

3.8 AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Lift, Table 1208.2

3.8

c_{Mlpha}^*	119.453374 112.969078 19.726978 6.4849787	-3.89460413 -2.8946061 -2.5952111 -1.9472535	-1.2997696 -1.11149738 97649075 78288043	56232521 49368636 39798115 34598115	28939462 28939462 289369462 1.20824494 1.90824494	17621243 15257940 15257998 18281399	1.00629406 1.09321604 1.08266754 1.08266754	04268390 02794100 02104918
$\overline{c}_{M\alpha}$	-80018.1684 -890.88867 -501.11556	-125.26293 -80.160626 -35.615167 -120.024299	-8.8880832 -6.5245475 -4.9905734 -3.1867628 -2.2071029	-1.8338800 -97108123 -78358185 -397858185		13145133 11238748 09748422 08562063	05091477 04099545 03324455	00806658 00338847 00205953
C _M h	-37 -128.657025 -12.437801 -9.3281251 -6.2183196	-4.6632879 -3.7301660 -2.4857042 -1.8631548 -1.4893731	-1. 2399783 -1. 0616647 -92777999 73999460	522446533 455475516 361494050	251179784 19082311 159754256 16975425	1.12402253 1.112472453 1.11841361 1.11070805	080440536 07540536 0491489	03475959 02415981 01790424
\overline{c}_{Mh}	0021 0021 0021 0021 0021 0021 0021 0021 0021 0021 0021 0021 0021 0021 0021 0021	02150343 02148609 02148597 02134194	02110283 02094818 02077049 02034729	01924105 01856588 01781555 01699534	01313689 01095545 00868319 00638004	. 000191487 . 00013865 . 00200933 . 00365833	.00782636 .00736129 .00564397	.00062910 00006521 .00025200
ប	00000 00000 00000 40040	00000	00000 00000 0000 00000	00000	00000 111100 40000	00000 00000 40000 00000	0000 4400 0000 0000	10.00

AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Moment, M Table 1208.2

$c_{L\sigma}^*$	-150.391101 -15.1395669 -10.130578 -7.5980721	-3.03995106 -2.03985106 -2.0372533 -1.52112933	-1.0153926 87105993 76290401 61170503 51114070	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		129897245 12988715 12084382 11337801	08549807 07542809 06718710	03434270 02260334 01699867
$\bar{c}_{L\alpha}$	-14961.714 -13740.4138 -1662.3952 -935.08865 -415.58400	-233.75738 -149.59764 -66.476925 -37.384706	-16.604640 -12.1904629 -9.3317414 -5.9655639	- 3. - 3. - 1. - 88985411 - 1. - 4.787493 - 1. - 2.287493 - 1. - 2.887493	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	25052819 21335137 18405791 16058453	1 . 0 0 9 1 9 0 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6	01465006 00639476 00369196
c _{Lh}	-70.133018 -35.066345 -23.377381 -17.532844 -11.688197	-8.7657648 -7.0122179 -4.6739013 -3.5044724	-2.3345092 -2.0000091 -1.7490051 -1.3973018	999455306 770077552 69129443	48805037 37485535 33535713 30321153		16632350 14970795 13654416 09141815	06706939 04531652 03389388
$ar{c}_{\mathrm{Lh}}$	02191623 021911812 021911826 02191067	02189287 02183323 02176853	02158433 02146514 02132812 02100155	02014613 01962276 01903992 01840130	01537368 01364227 01182046 00995103	00623842 00447509 00282158 00130829	.00348806 .00403338 .00356504	.00030318
G	00000 00000 00000 40040	00000 00000 00000 00000 00000	00000 00000 00000 00000	00000	00000 111100 40000	00000 00000 40000 00000		448 000 000

AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Lift, M Table 1208.2

CMa	137.014788 112.338480 19.2540029 6.1696071	13. 6274906 13. 7022857 12. 4688657 11. 8523614 11. 4827614	-1.2362524 -1.0603889 92858700 74428779	53426013 41812952 37764146	24405438 24182833 21675706 19663311		10012073 08791128 07806626	04024223 026394224 019839924
Č _M α	-7480.8491 -11870.1988 -831.18955 -467.53629	-116.87067 -74.790798 -33.230460 -18.684376 -11.951656	-8 - 29 4 11 67 - 1 8 - 1 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	-1. 51009 22 -1. 15264 96 90775054 73273650 50519036	36852315 28032463 22031774 17780779	12336702 10544278 09140951 08022360	047469 :: 03816185 03094291 01150406	00757682 00314489 00191824
CMh	-35.066454 -11.688526 -8.7662027 -5.8437701	.4.3624444.2.35655617 .2.3361309 .1.7511454	-1.1656280 99811401 87235171 69599017		203796694 18081653 16104329	 113221 113221 113260 11360 10535664 69664	08268573 07619198 07087814 04623565	03279137 02270125 01691033
\overline{c}_{Mh}	01826343 01826820 01826016 01825731	01823773 01822305 01817214 01810099	01789852 01776756 01761709 01725869	01632169 01574972 01511397 01441890	00929645 00736725 00541044	00161205 .00013738 .00173288 .00314115	.00671865 .00632664 .00485144	.00064510
a	00000 00000 00000 40240	00000	00000 00000 00000 00000	00000	00000 111193	00000	0000 440 0000 0000	10 20 20 00 00 00 00 00

4.0 Σ AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Moment, Table 1208.2

$c_{L\alpha}^{*}$	-27.355727 -13.677944 -9.1187184 -6.8391324	-3.4198871 -1.8245130 -1.3688508 -1.0955587			20188174 17806081 15955656 14473703	1.12835888 1.11368488 1.0604743 1.09937959	07484027 06612076 05901288	03008766 01986208 01488468
\bar{c}_{Llpha}	-12845.259 -3211.3048 -1427.2398 -802.81620	- 200 . 6940 - 128 . 6940 - 57 . 076792 - 32 . 099901	-114. -110. -10. -10. -10. -10. -10. -10. -1	-2.6089160 -1.9947363 -1.5737560 -1.2727298		21676533 18462416 15926159 13890959	07925763 06306103 05121955 02164512	01268198 00549760 00316922
$c_{ m rh}^*$	-61.054616 -30.527195 -20.351338 -15.263371	-7.6312338 -6.10412338 -4.0691843 -3.0512323 -4.0312323		86715306 75747945 67206279 60363761	42721791 37196511 32900678 29471340	224364 20177273 1.19369330 1.19369330 1.662330	14643183 13148491 11962894 07999632	05883120 03963788 02974759
$ ilde{c}_{\mathrm{Lh}}$	01507498 01507422 01507294 01507116	01505896 01504981 01501807 01497371	01484740 01476567 01467170 01444772	01386088 01350172 01310164 01266314	0009399 000939094 000813598 006814598	00428108 00305969 00191241 00086046	.002849220 .00287673 .00254209	.00030512 00012588 .00007985
a	00000 00000 00 19844	00000 00000 00000 000000	00000 00000 0000 0000 0000	00000	00000 111100 40000	00000 00000 00000 40000	0000 4400 0000 0000	200 200 200 200 200 200 200

4.5 AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Lift, M Table 1208.2

4.5

C,*	88. 94. 94. 94. 96. 96. 96. 96. 96. 96. 96. 96	. 121962 . 19977682 . 19897000 . 5499700	.1007130 94397087 82647893 66214123 55274375	24.14.13.22.24.14.13.22.24.23.23.24.23.23.24.23.23.23.23.23.23.23.23.23.23.23.23.23.	24205034 21316964 19070352 17268609	11 45 4 4 4 5 4 4 4 4 4 4 4 4 4 4 4 4 4	08755118 07706358 06861415 04601976	03522856 02320561 01736766
	7 H H B S	1 1 1 4 W G H H	4				iiii	
$\overline{c}_{\mathbf{M}\alpha}$	-6422.6243 -1605.6470 -713.61418 -401.40269	1 1 0 0 0 0 1 1 1 1 2 0 0 0 0 1 1 1 1 0 0 0 0	-7.1243353 -5.2310993 -4.0023455 -2.5574118	-1. 2995172 78255779 63189175 43634386		00911417 009149488 00923108 06943052	1.04067935 1.03259859 1.02642590	00656912 00268004 00162218
С _М h	-150.527270 -15.2537270 -17.631535 -5.08315350 -5.08315350	-3.08153 -8.00519916 -1.00519916 -1.0054083 -1.00583	1		200943114 115994063 12873994063	11753082 10812779 10028833 09371027	06670939 06670911 06168572	02880774 01975813 01487130
\vec{c}_{Mh}	01285622 01285622 012856128 012858018 8558018		01231231 01231232 01211921 01187339	01123 01103 01104 010404 009924 009924 009924		000109272 .00012108 .00123053 .00221227	.00473049 .00446430 .00342427	.00060963 00018786 00011978
ប	0000 0000 0000 0000 0000 0000	00000 00000 04400	00000 00000 00000 ww4n0	00000	00000 111100 40000	00000 %%%ww 40000	0000 44.87 0000	20.00

AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Moment, M Table 1208.2

$c_{\mathbf{L}lpha}^{*}$	1122. 1122. 1122. 12222461146. 1232461146. 13633601146.	13.1023960 11.6550180 11.2415943 93415943	82835648 71036705 62191993 49819932 41583187		18186791 16014014 14325771 12974075	10935568 10143143 09457074 08855272	1.066626 32 1.05892767 1.05267059	02678891 01772601 01325419
$\overline{c}_{\mathbf{L}oldsymbol{lpha}}$	-11280.326 -2820.0744 -1253.3612 -705.01151	-176.24578 -112.79389 -50.125376 -28.191410	-12.524334 -9.1991019 -7.0409170 -4.5029430	-2.2931846 -1.7537911 -1.3840551 -1.1196550	568110558 43376960 34187767 27633746		- 06979484 - 05546511 - 04502876 - 01917120	01119212 00483852 00277524
$c_{ m Lh}^*$		-6.7677685 -3.6088968 -2.7068914 -2.1068914	11. 8032418 11. 3515040 11. 3515040 11. 08025	76987519 67272109 59707398 53649006		21785743 18596883 17340556	13090287 11732988 10655140	05248354 03527689 02653507
\bar{c}_{Lh}	01082894 01082839 01082488 01082621	01081746 01081090 01078816 01075636	01066583 01060725 01053990 01037934	00995858 00970101 00941404 00909946	00760569 00584713 00584713 00491925	00307010 00218834 00135907 00059770	.00183850 .00211969 .00187279	.000027558 00014029 .00002784
a	00000 00000 00000 46844	00000 00000 00000 00000	00000 00000 00000 www.ano	00000	00000 40000 40000	00000 00000 00000 00000	0000 4425 0000	2118 050 000 000

5.0 AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Lift, M = Table 1208.2

C _M α	-29.704923 -14.852520 -7.4263772 -4.9510483	-3.7134229 -2.9708787 -1.9809105 -1.4860230 -1.1891670	99132608 85006446 74416412 59601079		21681562 19069120 17037031 15408239	129948230 111990773 11161440 10433873	0 6 8 6 8 4 9 3 4 1 0 6 1 2 7 3 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	03134721 02071658 01546276
$\bar{c}_{ m M} lpha$	1.5640 1.1410 1.626.01393 1.352.67674 1.56.6674	-88.119058 -56.393118 -25.058868 -14.091898	1 1 4 6 . 25 . 25 . 25 . 25 . 25 . 25 . 25 .	-1. -8. -1. -8. -1. -8. -1. -8. -1. -8. -1. -8. -1. -8. -1. -8. -1. -8. -1. -8. -1. -8. -1. -8. -1. -8. -1. -8. -8. -8. -8. -8. -8. -8. -8	28145761 21461554 16901117 13658988	09481000 08094835 07004247 06131123	. 03566117 . 02850829 . 02310637 . 00904016	00579115 00234973 00139794
C _M h	-27.072751 -13.536295 -9.0241061 -6.7679849	-3.3836678 -1.8040434 -1.3525617	90081707 67468881 53881596		18717766 16255661 14345425 12826186	10583674 09743190 09038687 08443776	0652351 05938351 05466115	02575205 01753139 01328377
\vec{c}_{Mh}	00902407 00902347 00902346 00902106		00884474 00878037 00870640 00853018 00831731	00806925 00778771 00747463 00713214	00551730 00460137 00364478 00267323	00077662 .00010071 .00090388 .00161588	.00345475 .00326542 .00250513	.00053362 -000020134
G	00000 00000 0 0000 48840	00000 00000 00000 00000	00000 00000 00000 00000	00000	00000 44000 40000	00000 00000 00000 40000	0000 4400 0000 0000	448 0.50 0.00 0.00

AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Moment, M = 5.0 Table 1208.2

$c^*_{\mathrm{L}lpha}$	-20.871655 -10.435859 -6.9572750 -5.2179934 -3.4787330	-2.6091240 -2.0873755 -1.3917602 -1.0440051	59635387 59706886 52263024 41847510	29960044 23370875 21069079 21069079	15166043 13326657 11897009 10752706	09030177 08362983 07787260 07284240	1.054747114 1.048491314 1.048489131	02200052 01460264 01089695
$ar{ ilde{c}}_{ ext{L}oldsymbol{lpha}}$	- 1 2 2 4 0 7	-142.30130 -91.070927 -40.473035 -22.763781 -14.566935	-10.114338 -7.4295717 -5.6870657 -3.6379074 -5.5248221	-1.8537055 -1.4181643 -1.1195978 90607404		- 155563810 - 113258416 - 1143538216 - 09968854	1 . 0 5 6 5 5 4 2 4 6 1 . 0 3 6 3 9 5 3 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	00908121 00392772 00223002
c_{Lh}^{*}	1.24.123 1.14.123 1.10.123 1.10.068168 1.376529	1.5. 5338995 1.2. 9510839 77016839	11. 26488568 11. 105648826 1. 1056159 1. 88395840 73609712	11111 		1111 1160 1160 1160 1160 1160 1160 1160	1.0814692 1.087669834 0.08759016	04327757 02899509 02185553
$ ilde{c}_{\mathrm{Lh}}$	00614895 00614864 00614812 00614740	006114245 006113814 006112586 006110786		00565605 00551011 00534748 00516915		00173944 000183849 00076079 00038480	.00107999 .00124342 .00109834	.00020340 00012452 00002777
ď	00000 00000 0 00000 4884	00000 00000 00000 00000	00000 00000 00000 00000	00000	00000 40000 40000	00000 00000 40000 00000	0000 4400 0000 0000	2000 2000 000 000

= 6.0AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Lift, M Table 1208.2

$c_{M\alpha}^*$	-24.771911 -12.785988 -6.1930594	11.0966005 11.65174068 11.6517859 11.6517859	82637921 70852407 62015834 49650619		15764039 15764039 14061068 12696975	1.10641474 1.09844574 1.09156650 1.08555482	1.06395607 1.05653064 1.05056185 1.03384488	02572239 01706858 01271124
Ē _M α	-4553.8062 -11138.4480 -505.97422 -284.60840	-71.148514 -45.533330 -80.234389 -11.379769 -7.2813546	-5.0550665 -2.0550665 -2.8414577 -1.8169131	92490270 70718743 55796585 45127143	22881404 17469661 13771839 11137986	06598033 06598033 05703109 04984943	02871166 02287657 01853799	00467674 00190683 00109771
c#h	-22. -11. -21. -2. -2. -3. -3. -3. -3. -3. -3. -3. -3. -3. -3	11111 1111 111		21418747 24341075 21858523 18128174	1111 111 1	00882629 007546299 007546242 007047455	05395520 04877545 04461288	02131889 01437536 01095572
Ċ _{Mh}	00512410 00512376 00512319 00512239	00511695 005112866 00509870 00507891	00502257 00498612 00494424 00484445	00458335 00442381 00424636 00405218	00313573 00261523 00207101 00151701	00043480 .00006740 .00052808 .00093743	.00200404 .00189799 .00145639	.00038180 00017325 00004574
q	00000 00000 00000 10000	00000 00000 04466	00000 0000 0000 0000 0000	00000	00000 1111466 40000	00000 00000 40000	0000 4480 0000 0000	200 000 000 000 000

AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Moment, M = 6.0 Table 1208.2

$c_{\mathbf{L}\alpha}^{*}$	-11.9988833 -18.99894311 -18.9989759 -2.996548	2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.	514968396 544998803 36021925 36021925	255772498 2008735498 18100644	11410784 10174498 09185122	07697329 07122214 06626882 06195079	1 0.446532955 0.04699298 0.08699298	01868576 01242356 00926790
$ar{c}_{\mathbf{L}oldsymbol{lpha}}$	-7660.5331 -1915.1308 -851.16743 -478.78025	-119.69261 -76.602097 -34.043567 -19.148086	-8.5084721 -6.2502768 -4.7846276 -3.0610418	-1. 56029 35 -1. 194239337 76316883 -529246011		- 13146468 - 11200075 - 09659204 - 08418875 - 06201563	1.04764961 1.03776482 1.03062657 1.01328501	00765377 00332072 00187305
c _{Lh}	-37.520975 -18.560459 -12.506941 -9.3801720 -6.2533842	-4.6899712 -3.7519082 -2.5011130 -1.8756681	11. 02501299 1. 03778693 1. 74948879 6848358	53472879 41529186 37345209	286574250 286574250 28659483 1.18490602 16779980	11.15.35.88.21.13.11.36.88.21.13.11.36.88.31.13.06.88.31.30.04.88.31.30.30.30.30.30.30.30.30.30.30.30.30.30.		03688026 02466393 01859777
$\bar{c}_{ m Lh}$	00382861 00382842 00382810 00382765		00377122 00375060 00372689 00367037			000108160 000046659 00046957 00019612	.00068610 .00078930 .00069712 00040893	00014615 00009738 00004368
G	00000 0000 0000 0000 0000	00000	00000 00000 00000 00000	00000	00000 44400 40000	00000 00000 00000 00000	0000 4400 0000 0000	2000 000 000 000

02183512 01451948 01081079
00392199 00161728 00091214
01822434 01222710 00932540
00027020
80.00 000 000

AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Moment, M = 7.0

Table 1208.2

C.*	-21.235854 -7.0786538 -5.3090139	-2.6545876 -2.1237184 -1.4159240 -1.0620601	70886178 60720423 53142686 42537547	26646845 23708572 23708572 21359642	1.15328398 1.113446150 1.11982150 1.10809904	09 04 57 73 08 36 3 3 59 07 77 54 21 07 26 27 95	05433839 04810001 04309066 02881786	02183512 01451948 01081079
$\overline{c}_{\mathbf{M}\alpha}$	1 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	- 59 . 8449 92 - 38 . 2997 35 - 17 . 020 473 - 9 . 5727 367 - 6 . 12 55 0 52		77894601 59580019 47026268 38049287	- 19324926 - 14765483 - 11647233 - 09423677	06542978 05580948 04820880 04210072	02410158 01916300 01552685	00392199 00161728 00091214
c _{wh}	118.3000478 16.2534416 14.6900477		532478069 5334525 46825872 37427618	286673072 2866730072 28669076 18886076 18887878	113180583 111489446 110175724 109127861	0 0 7 5 6 8 8 7 3 0 6 9 7 7 0 8 3 0 6 4 7 5 5 2 6 0 5 2 0 9 4 5 8	04603968 04143991 03775048 02491574	01822434 01222710 00932540
C _M h		00318605 00318351 00317471 00316240	00312739 00310473 00307870 00301666	00285433 00265433 00264475 00252396	00195353 00129004 00129004 00094443	. 000026839 . 0000334411 . 00059120	.000126385 .000119840 .00091967	.00027020 00013369 00006915
a	00000	00000	00000 00000 00000 00000	00000	00000 111400 40000	00000 00000 40000 00000	0000 4487 0000	200 200 000 000 000

0 8 11 Z Lift (Continued) COEFFICIENTS FLUTTER AERODYNAMIC 2 1208 ø Tabl

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c_{Mlpha}^*	-18.580823 -6.1936214 -6.1936314 -3.096852391	-2. 3226728 -11. 32826728 -1. 23881702 -2. 23921782 -2. 35921782	61962506 53118827 46487112 37205151		1.1337774 1.110444688 1.09417370 1.09417370	07872654 06762498 06315462	04727703 04188961 03756687 02510735	01898278 01263680 00941400
$\bar{c}_{I\!\!I\!\!I}$	-3310.9161 -827.72805 -367.87805 -206.93055	-51.731177 -14.713256 -8.2753615 -5.2955615	-3.6768759 -2.7008770 -2.0674209 -1.3224895	67388643 51556076 40703081 32941743	16748864 12803413 10103513 08176863	05677602 04841635 04180496 03648705	02080407 01651786 01338261 00562615	00337881 00140922 00078639
c*	-16.295922 -8.1479418 -5.4319400 -4.0739327	-1.6294663 -1.0862051 81454310 65152105		23195007 20274331 18000875 15180694	11493699 10087967 08889010 07979909	06624765 06108763 05670271 05294008	04016755 03605103 03275233	01592726 01065718 00811917
\vec{c}_{Mh}	00212182 00212168 00212145 00212112	00211887 00211718 00211134 00210316	00207990 00206485 00204756 0020635	001189849 001183856 001175982 00167893	000129965 0001083965 000085816 00062803	00017748 .00003214 .00032482 .00039643	.00084748 .00080421 .00061721 00044679	.00019453 00010111 00006866
ď	00000 00000 00000 148844	00000 00000 00000 00000	00000 00000 00000 00000	00000	00000 1111488 40000	00000 00000 00000 00000	0000 0000 0000 0000	110 115:00 20:00

AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Moment, M Table 1208.2

C _L α	11.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1	11. 14.56655 11. 14.0536655 14.0534466 14.05344666 14.05344666		20116231 17612110 15665449 14108933	101111000 08863175 07892938 07116595	05950375 05113800 05113800	03586269 03132623 02857967	01438375 00957788 00715080
\bar{c}_{Llpha}	-5837.3411 -1459.3411 -648.59211 -364.83241	- 91. 206944 - 25. 942244 - 14. 591859 - 3382543	1.6.4844473 1.3.64686946 1.2.334767 1.2.334767	11.1898762 10.91069232 10.71989592 10.58240225 10.4411014	29664301 22692836 17916544 14503122	10063815 08574352 07394146 06443302	03638111 028799997 02334539	00583945 00255008 00143069
c_{Lh}^{*}	-28.826374 -14.413174 -9.6087676 -7.2065602 -4.8043438	-3.6032267 -1.921625494 -1.4411418	96061454 82330274 72030846 57609208			11882638 10960489 10172234 09491288	07133110 067331567 05738801	02851743 01903906 01434527
\bar{c}_{Lh}	00177938 00177939 00177914 00177893	00177750 00177643 00177272 00176753	00175276 00174319 00173219 00170597	00163722 00159511 00154816 00149666	00125166 00111086 00096211 00080879	00050194 00035491 00021613 00008822	.00032586 .00037457 .00033077	.00007865 00005668 00003896
q	00000 00000 18848	00000 00000 04400	00000 00000 00000 00000	00000	00000 111198	00000 00000 40000	0000 4400 0000 0000	20.00

9.0 AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Lift, Table 1208.2

0 6

C _M a	16.515121 8.2575700 5.5050570 4.1288035	2.0644388 1.6515733 1.1011002 .82587899	. 5 5 5 6 6 8 7 9 3 7 4 7 2 5 0 5 7 4 7 4 7 4 7 4 7 4 7 4 7 4 7 4 7 4 7	23634590 20690817 118402182 116572051	.11870095 .104601908 .09859968 .08345944	.06972267 .06442132 .05986341 .05589897	.04186170 .03711604 .03331036	.01679772 .01118908 .00834151
Ē _M α	- 2918.65995 - 324.295646 - 182.41560 - 81.072846	4.1.2.3.4.4.5.4.6.6.2.3.4.4.5.4.4.5.4.5.4.5.4.5.4.5.4.5.4.5.4		59438675 45481047 35912969 29070193	- 14791266 - 11310690 - 08927962 - 07226796	05018091 036931999 03222104	01832048 01453161 01177277 00500433	
c <mark>#</mark>	-14.413183 -7.2065780 -4.8043705 -3.6032623	-1.8015778 -1.4412303 96074627 72048233 57630660	48017516 41149780 35997946 28782979	20530936 179949680 15940763 14332639	1.0192884 1.08898470 1.07892437 1.07089050	05889911 054323411 050428045 04707839	03563338 03191800 02894231 01917071	01414961 00945353 00719052
\overline{c}_{Mh}	00148281 00148211 00148254 00148252	00148075 00147957 00147549 00146978	00145354 00144303 00143095 00140217	00132684 00128684 00128957 00117348	00090847 00075769 00059982 00043886		.00059560	.00014332
ប	000000000000000000000000000000000000000	00000	00000 00000 00000 00000	000000000000000000000000000000000000000	00000 111100 40000	00000 00000 40000 00000	0000 440 000 000 000	2000 000 000 000

AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Moment, M Table 1208.2

$c_{\mathbf{L}\alpha}^{*}$	-12. -6.3323436 -4.2215696 -3.1661849 -2.1108045	-1.5831186 -1.2665106 84437665 63332049	36199908 316789908 2558071 25580768	18121875 15864180 14108911 12705285	1.09099251 1.079734751 1.07098086 1.06397665	05345800 045940875 04591888 04289109	03219097 02857644 02567209	01290556 00859658 00542150
\bar{c}_{Llpha}	- 5222.5431 - 1305.6350 - 580.28160 - 326.40792 - 145.06958	-81.601164 -83.210220 -13.055276 -13.549887	1. 2. 26 22 2 2 2 2 1 1 1 2 2 2 2 2 2 2 2 2 2	-1.0647980 81501386 64377072 52128951 36176327	26560107 20321392 16046557 12990990	09015877 00681641 06624156 05771963	03256745 02577195 02088797 00916769	00522524 00228775 00128249
c _{Lh}	-25.851587 -12.925784 -8.6171785 -6.4628726 -4.3085602	1.38313975 1.1.783309975 1.28334888 9334888	86152737 73839303 64603478 51671546	38887438 28665508 28792210 21474370	18388878 16074224 14274032 12834472 11657631	10678196 09850902 09143362 08531768	06409507 05709773 051512221	02562473 01710097 01287832
$ar{c}_{\mathrm{Lh}}$	001299249 001299249 001299249 00129923			00118935 00115877 00112468 00108728	00090933 00080705 00069897 00058755		.00023819 .00027374 .00024172 00014983	.00005952
d	00000 00000 00000 10000	00000	00000 00000 00000 00000	00000	00000	00000 00000 40000 00000	000 000 000 000 000 000	2000

AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Lift, M = 10.0 Table 1208.2

C.*	-14.862495 -7.4312541 -4.9541769 -3.7056405	-1.8578471 -1.4862938 99089971 74321375		21262231 165512033 16551575 184903724	10669360 09346970 08318441 07495275	06258613 05781672 05371857 05015651	1.03757177 1.03332836 1.02992688 1.01998460	01506859 01004089 00749091
\bar{c}_{Mlpha}	-2611.2711 -652.81704 -290.14036 -163.20352	-40.800145 -26.111740 -11.604675 -6.52720 -4.1770620	1.2.900440 1.1.631108860 1.04310887	53199991 32151020 26028340 8058340	13250459 10134837 08001342 06477576	04497953 038034571 03309301 02886344	01637838 01298185 01051685	00265003 00112525 00062371
CMh	-12.925790 -6.4628855 -4.30858955 -3.2314234 -2.1542607	-1.6156729 -1.86162306 -64616109 -51687109		18422317 16108710 14308312 12867273	09158410 07998849 07097498 06377460	05301717 04890617 04540179 04238385	03802440 02864418 02593778	01273119 00849848 00645347
Смh	00107713 00107706 00107694 00107677	00107563 00107478 00107181 00106767	00105588 001005888 001004888 001019488	00096389 00093046 000893255 00085253	1.00066004 1.000055049 1.000043578 1.00031878		.00043439 .00041259 .00031667	.00010804 00005919 00005147
a	00000 00000 00000 10000	00000 00000 00000 00000	00000 00000 0000 00000	00000	00000 111100 40000	00000 00000 40000 00000	0000 4485 0000	000 000 000

$c_{\mathbf{L}\alpha}^{*}$	-11.524564 -5.7622869 -3.8415300 -2.8811532	-1.4405962 -1.1524887 76835290 57629310		164485709 128430633 128832776 11554931	08271507 07246269 06449022 05811143		1.02920727 1.023393362 1.02330512	01170538 00779888 00582842
$\bar{c}_{\mathbf{L}lpha}$	-4727.0224 -1181.7550 -525.22399 -295.43814 -131.30539	-73.858923 -47.269418 -21.008179 -11.816747 -7.5624280	-5.2514416 -2.85719412 -2.95358999 -1.8900183	96393037 73784309 58884441 47198075	184053505 18405726 14535428 11768670	08168470 06959726 06001516 05229180	02948932 02332998 01890682 00831551	00472970 00207519 00116301
$c_{\rm Lh}^*$	-23.439780 -11.719883 -7.8132470 -5.8599268		78118196 66954036 58580348 46855858	11111 	111668 1129561166 1129561166 11651433 11651433		05819932 05182627 04673721 03116774	02326841 01552437 01168540
\bar{c}_{Lh}	00096857 00096857 00096844 00096833	00096755 00096697 00096495 00096213		00089126 00086835 00084281 00081480		00027302 00019281 00011706 00004721	.00017931	.000004595
a	00000 00000 0 10000	00000	00000 00000 00000 00000	00000	00000 444000 40000	00000 00000 40000 00000	0000 4486 0000	200000000000000000000000000000000000000

AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Lift, M = 11.0

C,*	-13.5510435 -4.5034872 -3.3776212	-1.6888307 -1.3510766 90074553 67558828		1.169333121.16933121.1503913121.1503913121.1503913121.150391312	09690159 08487325 07551786 06803099	05678639 05245181 04872892 04549467	03408672 03024764 02717128	01366546 00910776 00679917
Čμα	-2363.5109 -590.87717 -262.61167 -147.71874 -65.652366	-36.929135 -23.634383 -10.503764 -5.9080489	-2.6253993 -1.9286760 -1.4764776 -65583503	48166691 36863173 29114181 23572030	1.12004634 1.09183537 1.07251321 1.05870946	04076781 03475204 02943698 02314880	01481574 01173698 00950811	00239358 00102309 00056692
c,	-11.719887 -5.8599365 -3.9066162 -2.9299537	-1.4649478 -1.1719408 -78125367 -58589813		16710399 18613492 18981870 11676032	08315661 07265136 06448457 05795894	 0.44820282 1041282028 1.038530 33108531		01157230 00772087 00585418
[™] Zwh	00080714 00080708 00080700 00080687		00079122 00078551 00077894 00076329	000072332 000659727 00065940 00063889	00049466 00041256 00032658 00023887	00006692 .00001321 .00008695 .00015271	.00032648 .00031017 .00023808	.000008318 00004627 00004297
C)	00000 00000 0 00000 40040	0000 0000 0000 0000 0000 0000 0000	00000 0000 0000 0000 0000	00000	00000 11100 40000 40000	00000 00000 00000 00000	0000 4480 0000 0000	100 15:00 20:00

AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Moment, M = 11.0 Table 1208.2

c_{Llpha}^*	-10.571868 -5.2859378 -3.5239627 -2.6429764	-1.3215032 -1.70482853 52864321 -422936933	1.35247015 1.36214017 1.26439565 1.21156028	15119588 11767783 10595175 08836989	0581787 056407487 05908943 05323441	04444482 041105870 03815174 03562753	1.02673354 1.02374125 1.02134003	01071104 00713747 00533637
\overline{c}_{Llpha}	-4318.7189 -1079.6793 -479.85710 -269.91934 -119.96381	-67.479367 -43.186570 -19.193685 -10.796176 -6.9093303	-4.7979583 -3.5248688 -2.6985860 -1.7268807	88078169 67422100 53260828 43131813	21985191 16824552 13287818 10759274	07468483 06363380 05487199 04780879	02695032 02131701 01727412	00432116 00189926 00106440
$c_{\rm Lh}^*$	-21.443638 -10.721814 -7.1478695 -5.3608956	-2.6804255 -1.442270 -1.4295204 -1.0721079	711467722 61254652 53594412 42869057	26676332 23794976 21409423	15272778 11862431 10669180	08881058 08194497 07606920 07098615	05330147 04745121 04277829	02131109 01421593 01069596
$\overline{c}_{\mathrm{Lh}}$	00074456 000744456 00074446	00074378 00074333 00074178 00073961	00073345 00072944 00072484 00071388	00068515 00066754 00064791 00062638	00052390 000046497 000033847	00020982 000014812 00008984 00003609	.00013832 .000158932 .00014032	.00003612 00002727 00002308
a	00000 0000 00 19840	00000	00000 00000 00000 00000	00000	00000 44800 40000	00000 00000 40000	0000 4400 0000 0000	000 000 000

AERODYNAMIC FLUTTER COEFFICIENTS (Continued), Lift, W

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Moment,
(Concluded)
AERODYNAMIC FLUTTER COEFFICIENTS
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C.*	-12.383831 -6.1919193 -4.1279505 -3.0959673	11.5479991 1.82562700 1.61924260 1.49541700	41287075 35391265 30969709 24780237 20654675	15499281 13781437 12407486 10347231	08876175 07773129 06915203 06228666	05197765 04800518 04459441 04163246	1.03119793 1.02769171 1.02488277	1.01250330 1.00833426 1.00622525
C _M a		- 33. 7394 - 9. 59659 33 - 5. 39659 28 - 5. 3978391 - 5. 44172	1.2 39873 1.3490492 1.86320092 599288092	33688815 26608902 21545186	1.0975626 1.08397450 1.06631334 1.05369368	03728527 03178123 02742028 02390673	- 01352989 - 01071393 - 00867917	00218308 00093815 00052010
C#h	-10.721817 -5.3609031 -3.5739292 -2.6804404	-1.3401979 -1.0721449 -71473235 -53601689 -48878034	35728333 26789893 21425479	1.15292053 1.113374314 1.11882205 1.10688102	07615626 06655161 05908436 05311656	044118969 03785884 035334440	02663758 02378108 02149478	01060733 00707479 00535786
C _M h		00061960 00061911 00061740 00061702		00005558 000053603 00051461 00049116	00038029 00031718 00025107 00018362	00005136 .00001029 .00006703 .00011766	.00025154 .00023903 .00018347	.00006526
G	00000 00000 00000 10000	00000	00000 00000 00000 00000	00000	00000 111188 60000 40000	00000 00000 40000 00000	0000 440 7000 0000	2000 2000 0000 0000

SECTION 12 - AEROELASTIC PHENOMENA

REFERENCES

(Note: In this list APL/JHU designates the Applied Physics Laboratory of The Johns Hopkins University, and NACA designates the National Advisory Committee for Aeronautics.)

Ref. No.	<u>Title</u>
12-1	von Borbely, S.: "Concerning the Airforces Which Act on a Two-Dimensional Oscillating Airfoil Moving at Supersonic Speed," Z. Agnew. Math. Mech., Volume 22, No. 4, August 1942, pages 190-205. Translations: Chance-Vought Report 5339, April 13, 1945; British Ministry of Aircraft Production, RTP Translation 2019.
12-2	Smilg, Benjamin and Wasserman, Lee S.: "Application of Three-Dimensional Flutter Theory to Aircraft Structures," Army Air Corps Technical Report 4798, July 9, 1942.
12-3	Flax, A. H.: "Aeroelastic Problems at Supersonic Speeds," "SECOND INTERNATIONAL AERONAUTICAL CONFERENCE, MAY 24-27, 1949; CONVENED BY INSTITUTE OF AERONAUTICAL SCIENCES AND ROYAL AERONAUTICAL SOCIETY." Editor, Berneice H. Jarck, Institute of Aeronautical Sciences, Inc., New York, pages 322-360.
12-4	Garrick, I. E. and Rubinow, S. I.: "Theoretical Study of Air Forces on an Oscillating or Steady Thin Wing in a Supersonic Main Stream," NACA Technical Note 1383, 1947.
12-5	Miles, John W.: "The Oscillating Rectangular Airfoil at Supersonic Speeds," NAVORD Report 1170, July 21, 1949.
12-6	Miles, John W.: "On Harmonic Motion of Delta Airfoils at Supersonic Speeds," NAVORD Report 1234, June 13, 1950.
12-7	Watkins, Charles E.: "Effect of Aspect Ratio on the Air Forces and Moments of Harmonically Oscillating Thin Rectangular Wings in Supersonic Potential Flow," NACA Technical Note 2064, April 1950.
12-8	Flax, A. H. and Sherman, S.: "Ground Vibration Tests as a Basis for Flutter Analyses," Curtiss-Wright Report SD-145-S-2, July 30, 1943.
12-9	Garrick, I. E. and Rubinow, S. I.: "Flutter and Oscillating Airforce Calculations for an Airfoil in a Two-Dimensional Supersonic Flow," NACA Report 846 or Technical Note 1158, October 1946.
12-10	Barton, M. V.: "Stability of an Oscillating Airfoil in Super- sonic Flow," Journal of the Aeronautical Sciences, Vol- ume 15, No. 6, June 1948, page 371.
12-11	Cheilek, H. and Frissel, H.: "Theoretical Criteria for Single Degree of Freedom Flutter at Supersonic Speeds," Cornell Aeronautical Laboratory Report CAL-7A, May 8, 1947.

NAVORD REPORT 1488 (Volume 4) HANDBOOK OF	SUPERSONIC AERODYNAMICS
Reference Page 1200-2	References	1 January 1952

- Loring, S. J.: "General Approach to the Flutter Problem," Society of Automotive Engineers Journal, Volume 49, No. 2, August 1941, pages 345-355.
 Loring, S. J.: "Use of Generalized Coordinates in Flutter Analysis," Society of Automotive Engineers Journal, Volume 52, No. 4 (Transactions Section), April 1944, pages
- 12-14 Keller, E. G., Black, S. D., Czuba, T., and Pengelley, C. D.: "Supersonic Airforce Coefficients for Flutter Analysis," Curtiss-Wright Report P537-V-28, APL/JHU Report CM-469, April 22, 1948.

113-132.

- 12-15 Possio, C.: "L'Azione Aerodinamica sul Profilo Oscillante alle Velocita Ultrasonore," Acta. Pont. Acad. Sci., Volume I, No. 11, 1937, pages 93-106.
- Barton, M. V. and Poindexter, A. M.: "The Effect of the Variation of Some Structural Parameters on Binary Flutter in a Supersonic Flow," University of Texas Report UT/DRL-150, APL/JHU Report CM-417, March 1, 1946.
- Ruggiero, R. J.: "Investigation of Three Methods of Solving the Flutter Equations and Their Respective Merits," Journal of the Aeronautical Sciences, Volume 13, No. 1, January 1946, pages 3-22.

The following bibliography is suggested for additional information on the subjects covered in this section:

- 12-18
 Anderson, R. A.: "Determination of Coupled Modes and Frequencies of Swept Wings by Use of Power Series," NACA Report RM L7H28, October 20, 1947.
- 12-19
 Anderson, R. A. and Houbolt, J. C.: "Determination of Coupled and Uncoupled Modes and Frequencies of Natural Vibration of Swept and Unswept Wings from Uniform Cantilever Modes," NACA Technical Note 1747, November 1948.
- 12-20 Army Air Forces: "The Effect of Sweepback on the Critical Flutter Speed of Wings," Report TSEAC 5-4595-2-5, March 1946.
- 12-21 Army Air Forces: "The Effect of Sweepforward on the Critical Flutter Speed of Wings," Report TSEAC 5-4595-2-6, April 1946.
- 12-22 Army Air Forces: "German Experience with Aileron Compressibility Flutter," Report TSEAC 5-4595-2-11, May 1946.
- 12-23 Arnold, L.: "Vector Solution of the Three-Degree Case of Wing Bending, Wing Torsion, Aileron Flutter," Journal of Aeronautical Sciences, Volume 9, No. 13, November 1942, pages 497-500.
- 12-24 Bairstow, L.: "The Theory of Wing Flutter," Aeronautical Research Committee Report R and M 1041, 1927.
- 12-25 Barton, M. V.: "Stability of Supersonic Airflow on an Oscillating Airfoil," University of Texas Report UT/DRL-127, APL/JHU Report CF-753, August 13, 1947.

12-26	Barton, M. V.: "Two-Dimensional Torsional Flutter at Supersonic Speed," University of Texas Report UT/DRL-130, APL/JHU Report CF-761, August 26, 1947.
12-27	Barton, M. V.: "Coefficient Method for Solving the Flutter Frequency Equation," Journal of the Aeronautical Sciences, Volume 12, No. 2, pages 164-168, April 1945.
12-28	Barton, M. V. and Poindexter, A. M.: "Values of Some Aerodynamic Parameters Useful for Supersonic Flutter Studies," University of Texas Report UT/DRL-125, APL/JHU Report CF-720, July 10, 1947.
12-29	Bell, W. D.: "A Simplified Punch-Card Approach to the Solution of the Flutter Determinant," Journal of the Aeronautical Sciences, Volume 15, No. 2, February 1948, pages 121-122.
12-30	Bergen, W. B. and Arnold, L.: "Graphical Solution of the Bending-Aileron Case of Flutter," Journal of the Aeronautical Sciences, Volume 7, No. 12, October 1940, page 495.
12-31	Biot, M. A.: "Three-Dimensional Aerodynamic Theory Applied to Flutter Analysis," California Institute of Technology Report GALCIT-6, December 1, 1942.
12-32	Biot, M. A.: "Aero-Elastic Stability of Supersonic Wings, Report No. I: Chordwise Divergence, the Two-Dimensional Case," Cornell Aeronautical Laboratory Report CAL-1-E-1, APL/JHU Report CM-427, December 8, 1947.
12-33	Biot, M. A.: "Aero-Elastic Stability of Supersonic Wings, Report No. 2: An Approximate Treatment of Some Simple Three-Dimensional Cases," Cornell Aeronautical Laboratory Report CAL-1-E-1, APL/JHU Report CM-470, May 12, 1948.
12-34	Biot, M. A. and Wiancko, T. H.: "Theory of Electrical Flutter Predictor for Three Degrees of Freedom," California In- stitute of Technology Report GALCIT-8, January 1943.
12-35	Biot, M. A. and Wiancko, T. H.: "Electrical Network Model for Flexure-Torsion Flutter," California Institute of Technology Report GALCIT-3, September 1941.
12-36	Bleakney, W. M.: "Three-Dimensional Flutter Analysis," Journal of the Aeronautical Sciences, Volume 9, No. 2, December 1941, pages 56-63.
12-37	Bleakney, W. M. and Hamm, J. D.: "Vector Methods of Flutter Analysis," Journal of the Aeronautical Sciences, Volume 9, No. 12, October 1942, pages 439-451.
12-38	Bureau of Aeronautics: "A Vector Solution of the Flutter Stability Determinant," NAVAER Report SM-26, May 22, 1944.
12-39	Buxton, G. H. L. and Minhinnick, I. T.: "Expressions for the Rates of Change of Critical Flutter Speeds and Frequencies with Inertial, Aerodynamic and Elastic Coefficients," Royal Aircraft Establishment Report SME 3339.

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12-40	Cicala, P.: "Comparison of Theory with Experiment in the Phenomenon of Wing Flutter," NACA Technical Memorandum 887, February 1939.
12-41	Collar, A. R.: "Resistance Derivatives of Flutter Theory. Part II: Results for Supersonic Speeds," Aeronautical Research Council Report R and M 2139 (7470), January 1944; Royal Aircraft Establishment Report SME 3278.
12-42	Collar, A. R.: "The Expanding Domain of Aeroelasticity," Journal of the Royal Aeronautical Society, Volume 50, No. 428, August 1946, pages 613-636.
12-43	Collar, A. R.: "Aeroelastic Problems at High Speed," Journal of the Royal Aeronautical Society, Volume 51, No. 433, January 1947, pages 1-34.
12-44	Curtiss-Wright Corporation: "Structural Damping Coefficient in Flutter Calculations," Report 8458, August 18, 1941.
12-45	DiPaola, J.: "Arnold's Vector Method for Solving the Flutter Stability Determinant," Curtiss-Wright Report V-241-S-3, July 14, 1944.
12-46	Duncan, W. J.: "The Fundamentals of Flutter," Royal Aircraft Establishment Report Aero 1920, March 1944.
12-47	Duncan, W. J. and Collar, A. R.: "Calculation of the Resistance Derivatives of Flutter Theory," Aeronautical Research Committee Report R and M 1500, 1932.
12-48	Durling, B. J. and Huckel, V.: "Tables of Wing-Aileron Co- efficients of Oscillating Air Forces for Two-Dimensional Supersonic Flow," NACA Technical Note 2055, March 1950.
12-49	Flax, A. H.: "Three-Dimensional Wing Flutter Analysis," Jour- nal of the Aeronautical Sciences, Volume 10, No. 2, February 1943, pages 41-47.
12-50	Garrick, I. E.: "A Survey of Flutter," NACA University Conference on Aerodynamics - A Compilation of the Papers Presented at Langley Aeronautical Laboratory, Langley Field, Virginia, June 21-23, 1948, pages 289-304.
12-51	Jahn, H. A.: "A Review of British Work on Aerodynamic Derivatives for Flutter Prediction," Royal Aircraft Establishment Report SME 275, September 1944.
12-52	Jordan, P.: "Instationare Luftkrafte Beiwerte Bei Uberschall (Non-Stationary Air Force Coefficients at Supersonic Speed)," Aerodynamische Vesuchsanstalt Gottingen E. V. Institut fur Jastationare Vorgange J06, B45/J/8. Curtiss-Wright Translation U-46-14, August 23, 1946; Cornell Aeronautical Laboratory Translation by Jack Lotsof, May 1947.
12-53	Karp, S. N. and Weil, H.: "The Oscillating Airfoil in Com- pressible Flow," Air Materiel Command Report F-TR-1195-ND, Monograph III, Part II, June 1948.
12-54	Katz, H.: "Resume of Flutter Model Investigations," Bureau of Aeronautics Project Report 9.

Katz, H.: "Solution of the Stability Determinant," Bureau of Aeronautics Structures Memorandum 13.

12-55

12-56	Kussner, H. G.: "Status of Wing Flutter," NACA Technical Memorandum 872, January 1936.
12-57	Leppert, E. L., Jr.: "An Application of IBM Machines to the Solution of the Flutter Determinant," Journal of the Aeronautical Sciences, Volume 14, No. 3, March 1947, pages 171-174.
12~58	Miles, J. W.: "The Aerodynamic Forces on an Oscillating Airfoil at Supersonic Speeds," Journal of the Aeronautical Sciences, Volume 14, No. 6, June 1947, pages 351-358.
12-59	Pinkel, I. I.: "A Comparative Study of the Effect of Wing Flutter Shape on the Critical Flutter Speed," NACA Report ARR 3K15, November 1943.
12-60	Porter, F. P.: "A Simple Method for the Calculation of Natural Frequencies in Torsional Vibration," American Society of Mechanical Engineers Paper OGP-53-2, 1931.
12-61	Pugsley, A. G.: "A Simplified Theory of Wing Flutter," Aeronautical Research Committee Report R and M 1839, 1938.
12-62	Reissner, E. and Sherman, S.: "Compressibility Effects in Flutter," Curtiss-Wright Report SB-240-S-1, January 1944.
12-63	Scanlan, R. H. and Rosenbaum, R.: "INTRODUCTION TO THE STUDY OF AIRCRAFT VIBRATION AND FLUTTER," Macmillan, 1951.
12-64	Sezawa, K.: "The Nature of Wing Flutter as Revealed Through its Vibrational Frequencies," Journal of the Aeronautical Sciences, Volume 4, No. 1, 1936, pages 30-34.
12-65	Sezawa, K. and Kubo, S.: "The Nature of the Torsion-Aileron Flutter of a Wing as Revealed by Analytical Experiments," Tokyo Report 136, Volume 11, 1936, page 107.
12-66	Sherman, S., DiPaola, J. and Frissel, H. F.: "The Simplification of Flutter Calculations by Use of an Extended Form of the Routh-Hurwitz Discriminant," Journal of the Aeronautical Sciences, Volume 12, No. 4, October 1945, pages 385-392.
12-67	Targoff, W. P.: "The Associate Matrices of Bending and Coupled Bending-Torsion Vibrations," Journal of the Aeronautical Sciences, Volume 14, No. 10, October 1947, pages 579-582.
12-68	Teichmann, A.: "State and Development of Flutter Calculation," NACA Technical Note 1297, March 1951.
12-69	Theodorsen, T.: "General Theory of Aerodynamic Instability and the Mechanism of Flutter," NACA Report 496, 1935.
12-70	Theodorsen, T. and Garrick, I. E.: "Mechanism of Flutter - A Theoretical and Experimental Investigation of the Flutter Problem," NACA Report 685, 1940.
12-71	Theodorsen, T. and Garrick, I. E.: "Flutter Calculations in Three Degrees of Freedom," NACA Report 741, 1942.

12-72	Voigt, H.: "Wind Tunnel Investigations on Flexural-Torsional Wing Flutter," NACA Technical Memorandum 877, September 1938.
12-73	Williams, J.: "Methods of Predicting Flexure-Torsion Flutter," Aeronautical Research Committee Report 6574, March 20, 1943.
12-74	Wylie, J.: "Flexure-Torsion Binary Flutter," Civil Aeronautics Authority, Department of Commerce Report 22, 1941.
12-75	Zahm, A. F. and Bear, R. M.: "A Study of Wing Flutter," NACA Report 285, 1928.

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